

International GCSE Maths

Apart from questions 14a, 21 where the mark scheme states otherwise, the correct answer, unless clearly obtained from an incorrect method, should be taken to imply a correct method.

Question	Working	Answer	Mark	Notes
1	6 hrs 39 mins = 6.65 (hrs) or $6\frac{39}{60}$ or $6\frac{13}{20}$ or $\frac{133}{20}$ or 399 (mins)		3	B1
	Average speed = $\frac{429}{6.65}$ oe eg $\frac{429}{399} \times 60$			M1 Use of $S = D \div T$ (use of their time in hours) [allow $429 \div 6.39$ if B0 awarded]
		64.5		A1 Awrt 64.5
				Total 3 marks

2		3, 7, 8, 8 and one of 4 or 5 or 6	3	B3 For a list of 5 correct numbers (B2 for a list of 5 numbers with 2 of: median of 7, mode of 8, range of 5 B1 for a list of 5 or 6 numbers with 1 of: median of 7, mode of 8, range of 5)
				Total 3 marks

3	(a)	$520 - 465 (= 55)$ or $\frac{520}{465} (=1.118\dots)$	11.8	3	M1
		$\frac{"55"}{465} \times 100$ or $100 \times ("1.118" - 1)$ oe			M1
					A1 11.8 or better (11.827956...)
	(b)	0.12×550 oe (= 66)	484	3	M1 oe
		$550 - "66"$			M1
					A1
					Total 6 marks

4	(a)(i)		Correct line	1	B1 For $x = 1.5$ drawn
	(ii)		Correct line	1	B1 For $y = x$ drawn
	(iii)		Correct line	1	B1 For $x + y = 6$ drawn
	(b)		Correct region	1	B1 dep on B3 for correctly indicating the region R accept unlabelled or unshaded if clear. Shading can be 'in' or 'out'.
					Total 4 marks

5	(a)	$8x^2 + 20x - 6x^2 + 9x$	$2x^2 + 29x$	2	M1	3 correct terms or all 4 terms condoning incorrect signs
					A1	
(b)		eg $y^5 \times y^n = y^{19}$ or $y^{-1} \times y^n = y^{13}$ or $5 + n - 6 = 13$	14	2	M1	Use of 1 rule of indices or a correct linear equation in n
					A1	Accept y^{14}
(c)(i)		$7t - 2t < 7 + 8$ oe eg $5t < 15$ oe	$t < 3$	2	M1	Terms in t on one side and number terms the other side – may be in an equation or the incorrect inequality sign or an answer of $t = 3$ or eg $t \geq 3$
					A1	
	(ii)		open circle at $t = 3$ and a line with an arrow to the left	1	B1ft	ft their inequality Allow a line without an arrow if it reaches to at least -5 , with an arrow it can be any length
						Total 7 marks

6	(a)		1	1	B1
	(b)	$3 \times 10^{125} + 2 \times 10^{124}$ or digits 1024×10^n oe		3	M1
		32×10^{124} or $3 \times 10^{125} + 0.2 \times 10^{125}$ or $30 \times 10^{124} + 2 \times 10^{124}$			M1 oe ‘correct’ answer in incorrect form.
			3.2×10^{125}		A1
					Total 4 marks

7		$5 \times 398 (= 1990)$ or $6 \times 401 (= 2406)$		3	M1	Correct total for 5 or for 6 cocoa pods
		“2406” – “1990”			M1	(M2 for $398 + 6 \times 3$ or $401 + 5 \times 3$)
			416		A1	

8	$8^2 + 15^2 (= 289)$	167	5	M1
	$\sqrt{8^2 + 15^2} (= 17)$			M1
	$\pi \times \left(\frac{17}{2}\right)^2 (= 226.98\dots)$ or $0.5 \times 15 \times 8 (= 60)$			M1
	$\pi \times \left(\frac{17}{2}\right)^2 - 0.5 \times 15 \times 8$ (“226.98” – “60”)			M1
				A1 Accept answers which round to 167
				Total 5 marks

9		$2^4 \times 3^2 \times 5^4 \times 11 \times 13$	2	B2 (B1 for 12 870 000 or correct unsimplified product or $2^m \times 3^n \times 5^p \times 11 \times 13$ with at least 1 of m, n or p correct or for $2^4 \times 3^2 \times 5^4$)
				Total 2 marks

10	<p>eg $\frac{4}{5} \times \frac{3}{7} (= \frac{12}{35})$ oe or $0.24 \times \frac{4}{7} (= \frac{96}{700})$ oe or</p> <p>eg $\frac{4}{5} \times 3 (= \frac{12}{5} = 2.4)$ and $0.24 \times 4 (= \frac{24}{25} = 0.96)$ (or 3.36) or</p> <p>eg $\frac{4}{5} \times 300 (= 240)$ and $0.24 \times 400 (= 96)$ (or 336)</p>		3	M1
	<p>eg "$\frac{12}{35}$" + "$\frac{96}{700}$" $\left(= \frac{336}{700}\right)$ oe or</p> <p>"2.4" + "0.96" $\left(= \frac{3.36}{7}\right)$ oe or</p> <p>eg "$\frac{240}{300}$" + "$\frac{96}{400}$" $\left(= \frac{336}{700}\right)$ oe</p>			M1 or 0.48 or 48% or correct unsimplified fraction eg $\frac{84}{175}$
		$\frac{12}{25}$		A1 cao
				Total 3 marks

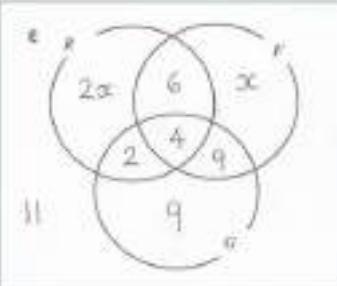
11	(definition of part: there are 3 parts: one part is the number, one part the letter t and one part the letter w Definition of terms: there are 6 terms: 2 number terms, 2 terms in t and 2 terms in w)		3	M1 indep	Fully correct cancellation of any two parts of their fraction at any stage of working
				M1 indep	correctly apply the negative power to the whole of their bracket (all parts or all terms) or correctly square all parts or terms of their bracket or correctly apply the negative power AND square of at least two parts (maybe 4 terms) of their bracket
		$4t^4w^2$		A1	Allow $(2t^2w)^2$ after the correct answer
	ALTERNATIVE			M2	2 correct terms (M1 for 1 correct term)
			4	A1	Allow $(2t^2w)^2$ after the correct answer
					Total 3 marks

12	13 – 4		2	M1	For selecting 4 and 13
		9		A1	
					Total 2 marks

13	(a) (i)		62	3	B1
	(a) (ii)		118		B1ft 180 – their (a)(i)
	(b)		62		B1
					Total 3 marks

14	(a)	<p>eg $20 \times \frac{9a-7}{5} - 20 \times \frac{3a-7}{4} = 20 \times 4.55 (= 91)$ or</p> <p>eg $4(9a-7) - 5(3a-7) = 20 \times 4.55$ or</p> <p>eg $\frac{4(9a-7)}{20} - \frac{5(3a-7)}{20} (= 4.55)$ or</p> <p>eg $\frac{4(9a-7) - 5(3a-7)}{20} (= 4.55)$</p>		3	<p>M1 For clear intention to multiply all terms by 20 (or 4×5) or a multiple of 20 oe or to express LHS as two fractions over 20 (or 4×5) or a multiple of 20 oe or as a single fraction with a denominator of 20 (or 4×5) or a multiple of 20 oe if expanded numerator, allow one error</p>
		eg $36a - 28 - 15a + 35 = 20 \times 4.55$ or $21a = 84$ oe			<p>M1 Expanding brackets and multiplying by denominator with no more than one sign error</p>
			4		<p>A1 dep on M1</p>
	(b)	$p^2 = \frac{ac+8}{3+c}$		4	<p>M1 for removing square root</p>
		$3p^2 + cp^2 = ac + 8$			<p>M1 for multiplying by denominator and expanding in a correct equation</p>
		$cp^2 - ac = 8 - 3p^2$ or $3p^2 - 8 = ac - cp^2$			<p>M1ft for gathering terms in c on one side and other terms the other side ft their equation dep on 2 terms in c and two other terms</p>
			$c = \frac{8-3p^2}{p^2-a}$		<p>A1 or $c = \frac{3p^2-8}{a-p^2}$</p>
					Total 7 marks

15	(a)	<p>$63 \div 1.5 (= 42)$ or a correct value written on FD scale (10 small squares = FD 10) or 10 squares = 1 parcel or 1 big square = 2.5 parcels oe eg area = $18 \times 5 + 15 \times 42 + 10 \times 24 + 10 \times 30 + 20 \times 8 (= 1420)$ $3.6 \times 1 + 3 \times 8.4 + 2 \times 4.8 + 2 \times 6 + 4 \times 1.6 (= 56.8)$ (at least 3 bars correct for any method of summing area)</p>		3	<p>M1 For use of area related to frequency eg showing a correct unambiguous value on the frequency density scale or calculating the area in some form</p>
		<p>$0.5 \times 18 + 63 + 1 \times 24 + 1 \times 30 + 2 \times 8$ $(9 + 63 + 24 + 30 + 16)$ oe eg “1420” $\div 10$ or “56.8” $\times 2.5$ oe</p>			<p>M1 Total of 5 frequencies with just one error or Area of bars with just one error, with correct calculation to give frequency</p>
			142		A1
	(b)	<p>$0.75 \times 24 (= 18) + 30 + 16 (= 64)$ oe Eg “their (a)” $- (9 + 63 + 0.25 \times 24) (= 64)$ (ft figures from (a) dep on M1 for (a))</p>		3	<p>M1ft (dep on M1 in (a))if working with small squares they may get eg $\frac{640}{1420}$</p>
		$\frac{"64"}{142} \times \frac{"63"}{141}$ (ft their value of 142 from (a))			<p>M1 64 must come from correct working allow $\frac{"64"}{142} \times \frac{"64"}{142}$ (ft their value of 142 from (a))</p>
			$\frac{672}{3337}$		A1 0.201 or better (0.20137...)
					Total 6 marks

16	(a)			3	B3	For all sections completed correctly (B2 for 5 or 6 sections correct (excl x), B1 for 3 or 4 sections correct (excl x))
	(b)	$2x + 6 + x + 2 + 4 + 9 + 9 + 11 = 80$ $(80 - 6 - 2 - 4 - 9 - 9 - 11) \div 3$		3	M1ft	ft their Venn diagram A correct equation to find x or subtracting all numerical values from 80 and dividing by 3 or other fully correct method to find x with all sections completed
		$x = 13$			A1	correct value for x
				38	B1	their $2x + 12$
						Total 6 marks

17	(a)	$\left(\frac{37+28}{2}\right) \times 20 (= 650)$		4	M1	Correct method to find area of trapezium
		$\sqrt{4.5^2 + 20^2} (= 20.5)$ oe			M1	Correct method to find slanted edge AB oe
		$2 \times '650' + 2 \times '20.5' \times 24 + 37 \times 24 + 28 \times 24$ $(2 \times '650' + 2 \times 492 + 888 + 672)$			M1	method to find the sum of the surface areas of at least 4 correct faces (ft their area of trapezium) ignore incorrect areas
			3844		A1	
	(b)	eg $\sqrt{24^2 + (37 - "4.5")^2} (= 40.4)$ $(AF =) \sqrt{24^2 + 20^2 + (37 - "4.5")^2} (= 45.08\dots)$		3	M1	Correct method to find diagonal from A to point on HE below F or AF
		$\tan x = \frac{20}{"40.4"} \text{ or } \sin x = \frac{20(\sin 90)}{"45.08"} \text{ or}$ $\cos x = \frac{"40.4"^2 + "45.08"^2 - 20^2}{2 \times "40.4" \times "45.08"}$			M1	Correct trig statement for finding the required angle
			26.3		A1	26.3 – 26.4
					Total 7 marks	

18	(a)			4	B1 $b = 14$
		(Gradient $AB = \frac{12}{5}$ oe or eg $\frac{10--2}{1--4}$ oe			M1 For the gradient of AB
		(Gradient $BC = -\frac{5}{12}$ oe			M1 Ft correct use of $m_1 \times m_2 = -1$ for <i>their</i> gradient of AB or $a = 2.5$ or $c = -9.5$
			$a = 2.5, c = -9.5$		A1 for $a = 2.5$ and $c = -9.5$
	(b)	$(AB =) \sqrt{(1--4)^2 + (10--2)^2}$ $(= \sqrt{5^2 + 12^2} (= 13))$		3	M1
		$(BC =) \sqrt{(19-1)^2 + (10-2.5)^2}$ $(= \sqrt{18^2 + 7.5^2} (= 19.5))$ or $\sqrt{(19-1)^2 + (10 - \text{their } a)^2}$ or $1.5 \times "13"$			M1 ft their value of a
			65		A1
					Total 7 marks

19	$(v =) 3t^2 + 10t - 8$		5	M1 For at least 2 terms differentiated correctly
	$3t^2 + 10t - 8 = 0$			M1 Their $v = 0$ dep on M1 could be implied by correct values
	$(3t - 2)(t + 4) (= 0)$ $(t =) \frac{2}{3}$ or $(t =) -4$			M1 dep on M1 for correct values for t or for $t = \frac{2}{3}$ or correct method to solve their 3 term quadratic equation: If factorising, allow brackets which when expanded give 2 out of 3 terms correct (If using formula or completing the square allow one sign error and some simplification – allow as far as eg $\frac{-10 \pm \sqrt{100+96}}{6}$ oe $3(t + \frac{5}{3})^2 - \frac{48}{3} = 0$)
	$(s =) \left(\frac{2}{3}\right)^3 + 5 \times \left(\frac{2}{3}\right)^2 - 8 \times \frac{2}{3} + 10$			M1 For $\frac{2}{3}$ (only) substituted into formula for s or for selecting the value from this substitution or for an answer of 7.185...
		$\frac{194}{27}$		A1 oe but numerator and denominator must be integers.
				Total 5 marks

20	<p>eg $0.5 \times x \times x \times \sin 60 \left(= \frac{\sqrt{3}}{4} x^2 = 0.433\dots x^2 \right)$ oe where $x = PQ$</p> <p>eg $0.5 \times 2n \times 2n \times \sin 60 \left(= \sqrt{3}n^2 = 1.732\dots n^2 \right)$ oe where $2n = PQ$</p> <p>or use $0.5 \times b \times h$ where $h = \sqrt{x^2 - (0.5x)^2} \left(= \frac{\sqrt{3}}{2} x \right)$ oe</p>	4	<p>M1 For expression for area of triangle [using $AB = x$ and $PQ = \frac{2}{3}x$ gives $\frac{\sqrt{3}}{9} x^2 = 0.192\dots x^2$] (correct expression in 1 variable eg PQ)</p>
	<p>eg $6 \times 0.5 \times 1.5x \times 1.5x \times \sin 60 \left(= \frac{27\sqrt{3}}{8} x^2 = 5.845\dots x^2 \right)$ oe</p> <p>eg $6 \times 0.5 \times 3n \times 3n \times \sin 60 \left(= \frac{27\sqrt{3}}{2} n^2 = 23.382\dots n^2 \right)$ oe or</p> <p>eg $2\left(\frac{1}{2} \times 1.5x \times 1.5x \times \sin 120\right) + 1.5x \times AE$ where</p> <p>eg $AE = \sqrt{(1.5x)^2 + (1.5x)^2 - 2 \times 1.5x \times 1.5x \times \cos 120}$</p> <p>$\left(= \frac{27\sqrt{3}}{8} x^2 = 5.845\dots x^2 \right)$ or use of $6 \times 0.5 \times b \times h$, finding h by Pythagoras</p>		<p>M1 for expression for area of hexagon [using $AB = x$ and $PQ = \frac{2}{3}x$ gives $\frac{3\sqrt{3}}{2} x^2 = 2.598\dots x^2$] (correct expression in 1 variable eg AB)</p>
	<p>eg $6 \times 0.5 \times 1.5x \times 1.5x \times \sin 60 - 0.5 \times x \times x \times \sin 60 = 72\sqrt{3}$ oe or</p> <p>$\left(\frac{27\sqrt{3}}{8} - \frac{\sqrt{3}}{4} \right) x^2 = 72\sqrt{3}$ or $(5.845\dots - 0.433\dots) x^2 = 124.7\dots$ or</p> <p>eg $6 \times 0.5 \times 3n \times 3n \times \sin 60 - 0.5 \times 2n \times 2n \times \sin 60 = 72\sqrt{3}$ oe</p> <p>$\left(\frac{27\sqrt{3}}{2} - \sqrt{3} \right) n^2 = 72\sqrt{3}$ or $(23.382\dots - 1.732\dots) n^2 = 124.7\dots$</p>	4.8	<p>M1 for a correct equation for shaded area (correct equation in 1 variable, eg PQ or x etc)</p>
			A1

			Total 4 marks
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21	$\frac{(5x-8)(5x+8)}{(5x+2)(x-3)} \times \frac{(x-5)(x-3)}{5x+8} \text{ or eg } \frac{(5x-8)(x-5)}{(5x+2)}(-(x-7))$		4 M2 For factorising at least 2 of the quadratics correctly – could be implied by 2 factors cancelled correctly (M1 For factorising at least 1 of the 3 quadratics correctly)
	$\frac{(5x-8)(x-5)-(x-7)(5x+2)}{5x+2} \text{ oe or}$ $\frac{5x^2 - 25x - 8x + 40 - (5x^2 - 35x + 2x - 14)}{5x+2} \text{ oe or}$ $\frac{(25x^2 - 64)(x^2 - 8x + 15) - (x-7)(5x^2 - 13x - 6)(5x+8)}{(5x^2 - 13x - 6)(5x+8)} \text{ oe or}$ $\frac{(5x-8)(x^2 - 8x + 15) - (x-7)(5x+2)(x-3)}{(5x+2)(x-3)} \text{ oe or}$ $\frac{(25x^2 - 64)(x-5) - (x-7)(5x+2)(5x+8)}{(5x+2)(5x+8)} \text{ oe}$		M1 (indep (ft if M2 awarded)) For writing the fractions over a common denominator with or without brackets removed – need not be in simplest form Could be written as 2 separate fractions over a common denominator
		$\frac{54}{5x+2}$	A1 dep on M3
			Total 4 marks

22		eg $(AD =) \sqrt{6^2 + 6^2 - 2 \times 6 \times 6 \times \cos(50)}$ ($= 5.07\dots$) or $2 \times 6 \sin 25$ ($= 5.07\dots$) or $\frac{6 \sin 50}{\sin 65}$ ($= 5.07\dots$) oe		6	M1	Correct expression for AD ie $AD = \dots$ or $x =$ oe
		eg $6 + 6 + \sqrt{6^2 + 6^2 - 2 \times 6 \times 6 \times \cos(50)}$ or $12 + "5.07\dots"$ $(= 17.07\dots$ or $17.1)$			M1	A correct statement of perimeter of triangle OAD
		eg $(\text{arc } BC =) \frac{50}{360} \times \pi \times 2 \times (6 + x)$ oe			M1	A correct statement for arc BC (condone missing brackets around $(6 + x)$ for this mark only)
		eg $2 \times "17.1" = 12 + 2x + \frac{50}{360} \times \pi \times 2 \times (6 + x)$ oe			M1	dep on M3 for a correct equation for x
		eg $2 \times 17.1 - 12 - \frac{30}{18} \pi = 2x + \frac{5x}{18} \pi$			M1	isolating terms in x in a correct equation
			5.89		A1	$5.88 - 5.89$
		Total 6 marks				