

International GCSE Maths

Apart from questions 5a, 10, 18a, 19, 22, 23, 24 (where the mark scheme states otherwise) the correct answer, unless clearly obtained from an incorrect method, should be taken to imply a correct method.

Question	Working	Answer	Mark	Notes
1	e.g. $\pi \times 8.2^2 (= 211.24\dots, \frac{1681}{25} \pi)$ or $1.5 \times 1000 (= 1500)$ or $\pi \times 8.2^2 \times 10 (= 2112.4\dots, \frac{3362}{5} \pi)$		3	M1 for a correct first step
	e.g. $(1.5 \times 1000) \div (\pi \times 8.2^2) (= 7.1009\dots)$ or $(1.5 \times 1000) \div "2112.4" \times 10 \text{ oe } (= 7.1009\dots)$ or $10 - ((\text{"}2112.4\text{"} - 1.5 \times 1000) \div (\pi \times 8.2^2)) (= 7.1009\dots)$			M1 for a complete method to find the depth of the water or an answer of 2.89 – 2.91
		7.1		A1 accept 7.09 – 7.11
				Total 3 marks

2	Ext $\angle = 180 - 162 (= 18)$ oe or $\frac{(n-2)180}{n} = 162$ oe		3	M1
	$360 \div "18" \text{ oe } \mathbf{or} 18n = 360$			M1
		20		A1
				Total 3 marks

6	(a)	$4.25 \times 0.08 (= 0.34)$ oe		3	M1	M2 for 4.25×1.08 oe
		$4.25 + "0.34"$			M1	
			4.59		A1	SC: B1 for $4.25 \times 0.92 (= 3.91)$ oe
	(b)	$9.45 \div 108 (= 0.0875)$ oe		3	M1	M2 for $9.45 \div 1.08$
		$9.45 \div 108 \times 100$ oe			M1	
			8.75		A1	
					Total 6 marks	

7	$7.5^2 - 6^2 (= 20.25)$		4	M1	OR for a correct trig statement involving one of the angles e.g. $\cos BAM = \frac{6}{7.5}$ or $\sin ABC = \frac{6}{7.5}$ where M is the midpoint of BC	
	$\sqrt{7.5^2 - 6^2} (= 4.5)$			M1	OR for a method to find one of the angles in the triangle e.g. $BAM = \cos^{-1}\left(\frac{6}{7.5}\right) (= 36.8\dots)$ or $ABC = \sin^{-1}\left(\frac{6}{7.5}\right) (= 53.1\dots)$	
	"4.5" $\times$ 6 oe			M1	for a complete method to find the area of triangle ABC e.g. $2 \times \frac{1}{2} \times 7.5 \times 6 \times \sin("36.8")$ oe or $2 \times \frac{1}{2} \times 7.5 \times \sqrt{7.5^2 - 6^2} \times \sin("53.1")$ oe	
		27		A1	cao	
					Total 4 marks	

8	$10 \times 79.2 (= 792) \text{ or } 3 \times 68 (= 204)$		3	M1
	$(10 \times 79.2 - 3 \times 68) \div 7$			M1
		84		A1
				Total 3 marks

9 (a)		t^6	1	B1
(b)		w^{12}	1	B1
(c)		$125x^3y^6$	2	B2 (B1) for 2 correct terms as part of a product
				Total 4 marks

10	$22 \times 60 \times 60 (= 79\,200) \text{ oe or } 22 \div 1000 (= 0.022) \text{ oe}$		3	M1 for converting from m/s to m/h or from m to km	M2 for $22 \times 3.6 \text{ oe}$
	$22 \times 60 \times 60 \div 1000 \text{ oe}$			M1 for a complete method	
		79.2		A1 oe, dep on at least M1	
				Total 3 marks	

11	$15 - 3 : x - 3 = 2 : 7$ or $(15 - 3) \div 2 (= 6)$	$(n =) (15 - 3) \div \frac{2}{2+7} (= 54)$ where n is the total age 3 years ago		3	M1	M2 for $\frac{(15-3) \times 7}{2} (= 42)$
	$\frac{x-3}{15-3} = \frac{7}{2}$ oe or $7 \times "6" (= 42)$	$"54" \times \frac{7}{2+7} (= 42)$			M1	
				45		A1
						Total 3 marks

12	$105 \div (5 \times 4) (=5.25)$ oe or $105 \div (4 \times 3) (=8.75)$ oe or $105 \div (3 \times 5) (=7)$		3	M1
	"8.75" – "5.25"			M1 dep on previous M1. If M1 gained and they have worked out 3 pressures, award M1 for their highest minus their lowest.
		3.5		A1 oe
				Total 3 marks

13 (a)			1	B1 Professional judgment required, eg allow double shading if meaning clear.
(b)		$(D \cup E) \cap F$	1	B1 oe eg $(D \cap F) \cup (E \cap F)$
				Total 2 marks

14 (a)		0.7, 0.2, 0.8, 0.1, 0.9	2	B2 oe, all correct (B1) 2 or 3 or 4 correct probabilities
(b)	$0.3 \times "0.2" (= 0.06)$ or $0.7 \times "0.1" (= 0.07)$ oe		4	M1 ft from (a) dep on probabilities being between 0 and 1, OR $0.3 \times "0.8" (= 0.24)$ or $0.7 \times "0.9" (= 0.63)$ oe
	$0.3 \times "0.2" + 0.7 \times "0.1" (= 0.13)$ oe or $"0.06" \times 200 (= 12)$ or $"0.07" \times 200 (= 14)$			M1 ft from (a), OR $0.3 \times "0.8" + 0.7 \times "0.9" (= 0.87)$ oe or $"0.24" \times 200 (= 48)$ or $"0.63" \times 200 (= 126)$
	$"0.13" \times 200$ oe or $"12" + "14"$			M1 ft from (a), $200 - "0.87" \times 200$ oe or $(1 - "0.87") \times 200$ or $200 - "48" - "126"$
		26		A1 cao
				Total 6 marks

15	(Gradient of L_1) $6 \div 2 (=3)$		4	M1	could be seen as part of an equation. Ignore constant term if candidate rearranges L_1
	$m \times "3" = -1$ or $m = -\frac{1}{"3"}$			M1	for use of $m_1 m_2 = -1$ could be seen as part of an equation
	$-1 = "-\frac{1}{3}" \times 9 + c$ or $y - -1 = "-\frac{1}{3}"(x - 9)$ or $c = 2$			M1	
		$y + \frac{1}{3}x = 2$		A1	oe in required form eg $3y + x = 6$, $6y + 2x = 12$ etc
				Total 4 marks	

16	(a)	$3 \times 4t^2 - 2 \times 6t + 5$		2	M1	For 2 terms correct
			$12t^2 - 12t + 5$		A1	Fully correct
	(b)	$24t - 12$		3	M1	Method to differentiate their v, ft a 3 term quadratic expression from (a)
		$"24t - 12" = 6$			M1	ft if previous M1 awarded
			0.75		A1	oe
					Total 5 marks	

17	(a)	e.g. one correct value on the vertical scale e.g. 1 at 1 cm high or $1 \text{ cm}^2 = 5 \text{ passengers}$ or 5 small squares = 1 passenger or (FD $\Rightarrow$) $24 \div 20 (= 1.2)$		3	M1	For a correct scale on the vertical axis or a $1 \text{ cm} \times 1 \text{ cm}$ square = 5 passengers or other correct scale or one correct product or frequency (other than the 24) or (FD $\Rightarrow$) $24 \div 20 (= 1.2)$
		$10 \times 0.4 (= 4)$ $10 \times 1.8 (= 18)$ $5 \times 6.4 (= 32)$ $15 \times 2 (= 30)$ $20 \times 0.8 (= 16)$			M1	At least 3 correct products or frequencies (other than the 24) stated (could be seen on diagram)
			124		A1	
	(b)	e.g. $0.25 \times 24 + 20 \times 0.8 (= 22)$ or " 1.2 " $\times 5 + 20 \times 0.8 (= 22)$		2	M1	ft from (a)
			$\frac{"22"}{"124"}$		A1ft	oe (0.17(741...))
					Total 5 marks	

18	(a)	$(x + 2)(2x + 3) = 2x^2 + 3x + 4x + 6$ $(2x + 3)(x - 7) = 2x^2 - 14x + 3x - 21$ $(x + 2)(x - 7) = x^2 - 7x + 2x - 14$		3	M1	For multiplying a pair of brackets and getting 3 out of 4 terms correct.
		$(2x^2 + 7x + 6)(x - 7) = 2x^3 - 14x^2 + 7x^2 - 49x + 6x - 42$ $(2x^2 - 11x - 21)(x + 2) = 2x^3 + 4x^2 - 11x^2 - 22x - 21x - 42$ $(x^2 - 5x - 14)(2x + 3) = 2x^3 + 3x^2 - 10x^2 - 15x - 28x - 42$			M1dep	For multiplying the product of the first 2 brackets (ft from the 1 st stage) by the 3 rd bracket, and getting at least 3 out of 6 or 4 out of 8 terms correct
			$2x^3 - 7x^2 - 43x - 42$		A1	Fully correct. isw extra work as long as correct e.g. $x(2x^2 - 7x - 43) - 42$
		Alternative (all in one method)				
		$(x + 2)(2x + 3)(x - 7) =$ $2x^3 - 14x^2 + 3x^2 - 21x + 4x^2 - 28x + 6x - 42$			M2 (M1)	For at least 6 out of 8 correct terms for 4 or 5 out of 8 correct terms
			$2x^3 - 7x^2 - 43x - 42$		A1	
	(b)	$p^2(2m - y) = x + m$ $2p^2m - p^2y = x + m$		3	M1	Multiplying by denominator and expanding bracket
		e.g. $2p^2m - m = x + p^2y$ $m(2p^2 - 1) = x + p^2y$			M1	Collect terms in m and factorise in a correct equation
			$m = \frac{x + p^2y}{2p^2 - 1}$		A1	oe eg $m = \frac{-x - p^2y}{1 - 2p^2}$ must have $m =$

				Total 6 marks
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19	$a + 24d = 44.5$		5	M1	oe
	$\frac{30}{2}(2a + (30 - 1)d) = 765$ oe, eg $(15(2a + 29d) = 765)$, $(2a + 29d = 51)$, etc			M1	oe (may be simplified)
	e.g. $2(44.5 - 24d) + 29d = 51$ oe or $\underline{2a + 48d = 89}$ $\underline{2a + 29d = 51}$ oe			M1	dep on M2, a complete method to eliminate one variable, allow one arithmetic error
		26.5		A2	dep on M2, oe
				(A1)	dep on M2. If not A2, award A1 for $a = -3.5$ or $d = 2$
				Total 5 marks	

20	125 or 10^{21n}		3	M1
	125×10^{21n}			M1
		$1.25 \times 10^{21n+2}$		A1
				Total 3 marks

21	(a)(i)		(9, 3)	1	B1
	(a)(ii)		(4, 9)	1	B1
	(b)		$a = -2, b = 3$	2	B2 or $a = 2, b = -3$ (B1) for $a = -2$ or $a = 2$ or $b = 3$ or $b = -3$
					Total 4 marks

22	$2x^2 + 3(2x + 1)^2 = 5$		5	M1 $2\left(\frac{y-1}{2}\right)^2 + 3y^2 = 5$
	eg $14x^2 + 12x - 2 = 0$ or if completing the square, allow $14x^2 + 12x = 2$ oe			A1 $7y^2 - 2y - 9 = 0$ or if completing the square, allow $7y^2 - 2y = 9$ oe
	eg $(7x - 1)(x + 1)$ or $(7x - 1)(2x + 2)$ eg $\frac{-12 \pm \sqrt{12^2 - 4 \times 14 \times -2}}{2 \times 14}$ oe eg $7\left(\left(x + \frac{3}{7}\right)^2 - \frac{9}{49}\right) = 2$ oe			M1 ft as long as M1 awarded and 3 term quadratic eg $(7y - 9)(y + 1)$ eg $\frac{2 \pm \sqrt{(-2)^2 - 4 \times 7 \times -9}}{2 \times 7}$ oe eg $7\left(\left(y - \frac{1}{7}\right)^2 - \frac{1}{49}\right) = 9$ oe
	$x = \frac{1}{7}, x = -1$ (need both)			A1 $y = \frac{9}{7}, y = -1$ (need both)
		$x = \frac{1}{7}, y = \frac{9}{7}$ $x = -1, y = -1$		A1 Dep on M1 Must be paired correctly Must be 3 sf or better (0.142857...) (1.28571...)
				Total 5 marks

23	$ABF = 180 - x$ or $CDF = 180 - x$		4	M1 for finding an expression for ABF or CDF . May be seen on diagram.
	$FDE = 180 - (180 - x) (= x)$ AFB or $ACE = 180 - (180 - x) - 54 (= x - 54)$ DFE or $ACE = 180 - x - 32 (= 148 - x)$ e.g. $54 + y + 180 - x = 180$ where $AFB = y$ $32 + y + (180 - (180 - x)) = 180$ where $DFE = y$			M1 method to find FDE and AFB or method to find FDE and DFE or method to find ACE or method to find FDE and an equation for AFB e.g. $54 + y + 180 - x = 180$ where $AFB = y$ or method to find FDE and an equation for DFE e.g. $32 + y + (180 - (180 - x)) = 180$ where $DFE = y$ May be seen on diagram.
	e.g. $32 + x + x - 54 = 180$ or $54 + 180 - x + 148 - x = 180$ or $x - 54 = 148 - x$ oe or $54 + y + 180 - x = 180$ and $32 + y + (180 - (180 - x)) = 180$ where $AFB = DFE = y$			M1 for setting up an equation or a pair of correct simultaneous equations to solve for x
		101		A1 dep on at least M1
				Total 4 marks

24	$\overrightarrow{AP} = \frac{3}{4} \times 2\mathbf{c} (= \frac{3}{2}\mathbf{c})$ oe		5	M1 For $\overrightarrow{AP} = \frac{3}{2}\mathbf{c}$ oe, eg could be part of $\overrightarrow{OP} = \mathbf{a} + \frac{3}{2}\mathbf{c}$ oe or on diagram
	$\overrightarrow{AC} = \mathbf{c} - \mathbf{a}$ oe or $\overrightarrow{CA} = \mathbf{a} - \mathbf{c}$ oe			M1
	$\overrightarrow{OQ} = \mathbf{c} + n(\mathbf{a} - \mathbf{c})$ or $\overrightarrow{OQ} = \mathbf{a} + n(\mathbf{c} - \mathbf{a})$ or $\overrightarrow{QP} = n(\mathbf{a} - \mathbf{c}) + \frac{3}{2}\mathbf{c}$			M1
	$\frac{n}{1-n} = \frac{2}{3} \Rightarrow n = \frac{2}{5}$ oe or $\frac{1-n}{n} = \frac{2}{3} \Rightarrow n = \frac{3}{5}$ oe or $\frac{n}{\frac{3}{2}-n} = \frac{2}{3} \Rightarrow n = \frac{3}{5}$ oe			M1
		3 : 2		A1 oe, dep on M3
				Total 5 marks

25	e.g. $(220 - 180) + (360 - 280) (= 120)$		5	M1 for a method to find angle XYZ. Could be seen on a diagram
	$XZ = \sqrt{3.5^2 + 6^2 - 2 \times 3.5 \times 6 \times \cos("120")}$ ($= 8.3...$ or $\frac{\sqrt{277}}{2}$)			M1
	$\frac{\sin YXZ}{6} = \frac{\sin("120")}{"8.32..."}$			M1 or $6^2 = 3.5^2 + "8.32"{}^2 - 2 \times 3.5 \times "8.32" \times \cos YXZ$
	$YXZ = \sin^{-1}\left(\frac{6 \sin("120")}{"8.32..."}\right)$ ($= 38.6...$)			M1 or $YXZ = \cos^{-1}\left(\frac{3.5^2 + "8.32"{}^2 - 6^2}{2 \times 3.5 \times "8.32"}\right)$ ($= 38.6...$)
		241.4		A1 accept 241.2 – 241.4
				Total 5 marks