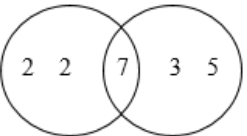


| Question | Working | Answer | Mark | Notes |
|--|--|----------------|------|---|
| Apart from questions (where the mark scheme states otherwise) the correct answer, unless clearly obtained by an incorrect method, should be taken to imply a correct method | | | | |
| 1 | (a) $\frac{5+13}{2}$ or $\frac{-4+1}{2}$ | | 2 | M1 for a correct method to find one coordinate or for one coordinate correct or for $(-1.5, 9)$ |
| | | $(9, -1.5)$ | | A1 oe |
| | (b) | -3 | 1 | B1 |
| | (c) | No with reason | 1 | B1 No (oe) and e.g. line goes through $(100, -298)$ or $(101.3(3..), -302)$ or $\left(\frac{304}{3}, -302\right)$ or $(3 \times 100) - 302 = -2$ not $(+)2$ |
| | | | | Total 4 marks |

| | | | | |
|---|--|-----|---|---|
| 2 | <p>28, 56, 84, 112... and 105, 210, 315, 420...</p> <p>or</p> <p>2, 2, 7 and 3, 5, 7</p> <p>or</p>  <p>or $\frac{28 \times 105}{7}$ or 2, 2, 3, 5, 7 oe</p> | | 2 | <p>M1 for any correct valid method e.g.</p> <p>for starting to list at least four multiples of each number</p> <p>or 2, 2, 7 and 3, 5, 7 seen (may be in a factor tree and ignore 1)</p> <p>or a fully correct Venn diagram</p> |
| | | 420 | | A1 cao |
| | | | | Total 2 marks |

| | | | | | |
|----------|--|--|----------|----------|--|
| 3 | | E.g. $12 \times 9 (=108)$ or $(9 - 6) \times x (= 3x)$ | | 4 | M1 for one correct relevant area |
| | | E.g. $129 - '108' (= 21)$ or $'108' + '3x' = 129$ | | | M1 (dep on M1) for 129 used correctly with another area or for a correct equation (ft) with bracket(s) expanded |
| | | E.g. $'21' \div (9 - 6)$ or $x = \frac{129 - '108'}{9 - 6}$ | | | M1 for a complete method |
| | | | 7 | | A1 Accept 7 cm |
| | | | | | Total 4 marks |

| | | | | | |
|----------|-----|--|----------------|---|---|
| 4 | (a) | | $3 < w \leq 4$ | 1 | B1 |
| | (b) | $(12 \times 2.5) + (16 \times 3.5) + (9 \times 4.5) + (2 \times 5.5) + (1 \times 6.5)$ or $30 + 56 + 40.5 + 11 + 6.5 (= 144)$ | | 4 | M2 for at least 4 correct products added (need not be evaluated) or If not M2 then award M1 for consistent use of value within interval (including end points) for at least 4 products which must be added or correct midpoints used for at least 4 products and not added |
| | | $[(12 \times 2.5) + (16 \times 3.5) + (9 \times 4.5) + (2 \times 5.5) + (1 \times 6.5)] \div 40$ or '144' $\div 40$ | | | M1 (dep on at least M1) Allow division by their Σf provided addition or total under column seen |
| | | | 3.6 | | A1 oe |
| | (c) | $\frac{2}{40} + \frac{1}{40}$ | | 2 | M1 for $\frac{a}{40}$ where $0 < a < 40$ or $\frac{3}{b}$ where $b > 3$ where a and b are integers |
| | | | $\frac{3}{40}$ | | A1 0.075 oe |
| | | | | | Total 7 marks |

| | | | | | | |
|----------|--|--|----|----------|--------------------------|--|
| 5 | | $120 \div (3 + 5) (= 15)$ | | 6 | M1 | M2 for $\frac{3}{8} \times 120 (= 45)$ or $\frac{5}{8} \times 120 (= 75)$ oe |
| | | '15' \times 3 (= 45) or '15' \times 5 (= 75) | | | M1 | |
| | | '45' \div 3 (= 15) or '45' \div 3 \times 2 (= 30) | | | M1 | |
| | | '75' \times $\frac{16}{25}$ (= 48) or '75' \times $\frac{9}{25}$ (= 27) | | | M1 | |
| | | E.g. ('45' \div 3 \times 2) + ('75' \times $\frac{9}{25}$) oe or '27' + '30' or ('75' - '48') + ('45' - '15') | | | M1 for a complete method | |
| | | | 57 | | A1 | |
| | | | | | | Total 6 marks |

| | | | | | | |
|----------|-----|--|--------------------|---|----|----------------------|
| 6 | (a) | | 0.000 78 | 1 | B1 | |
| | (b) | 22 500 000 oe e.g. 22.5×10^6 or 2.25×10^n $n \neq 7$ | | 2 | M1 | |
| | | | 2.25×10^7 | | A1 | |
| | | | | | | Total 3 marks |

| | | | | | |
|---|-----|--|-----------------|---|---|
| 7 | (a) | $m^2 - 8m + 5m - 40$ | | 2 | M1 for any 3 correct terms or for 4 out of 4 correct terms ignoring signs for $m^2 - 3m \dots$ or for $\dots - 3m - 40$ |
| | | | $m^2 - 3m - 40$ | | A1 |
| | (b) | | $5y(1 + 4y)$ | 2 | B2 If not B2 then award B1 for $5(y + 4y^2)$ or $y(5 + 20y)$ or $5y(a + 4y)$ where a is an integer and $a \neq 0$ or $5y(1 + by)$ where b is an integer and $b \neq 0$ |
| | (c) | | 1 | 1 | B1 |
| | (d) | E.g. $6x - 15$ or $12x - 30$ oe | | 4 | M1 for expansion of a correct bracket |
| | | $2 \times 3(2x - 5) = 9 - x$ oe or $2(6x - 15) = 9 - x$ oe or $3(2x - 5) = \frac{9}{2} - \frac{x}{2}$ oe | | | M1 for removal of fraction or separating fraction (RHS) in an equation |
| | | $12x + x = 9 + 30$ oe or $6x + \frac{x}{2} = \frac{9}{2} + 15$ oe | | | M1 ft (dep on 4 terms) for terms in x on one side of equation; number terms on the other |
| | | | 3 | | A1 dep on at least M2 awarded |
| | | | | | Total 9 marks |

| | | | | | |
|----------|--|--|--|---|---|
| 8 | | | Trapezium with vertices at (6, 3) (8, 3) (8, 6) (4, 6) | 2 | B2 If not B2 then award B1 for shape of correct size and orientation or 3 or 4 points plotted correctly |
| | | | | | Total 2 marks |

| | | | | | | |
|----------|--|--|------|---|---|---|
| 9 | | $\cos 63 = \frac{24.3}{(PQ)}$ or $\sin 27 = \frac{24.3}{(PQ)}$ or $\frac{(PQ)}{\sin 90} = \frac{24.3}{\sin 27}$ or $\frac{\sin 90}{(PQ)} = \frac{\sin 27}{24.3}$ oe | | 3 | M1 for a correct trigonometric ratio | M2 for $(RQ =) 24.3 \times \tan 63 (= 47.6914..)$ and $(PQ =) \sqrt{47.6914^2 + 24.3^2}$ oe |
| | | $(PQ =) \frac{24.3}{\cos 63}$ or $(PQ =) \frac{24.3}{\sin 27}$ or $(PQ) = \frac{24.3}{\sin 27} \times \sin 90$ | | | M1 for a correct rearrangement for PQ | |
| | | | 53.5 | | A1 Accept 53.5 - 53.53 | |
| | | | | | | Total 3 marks |

| | | | | |
|-----------|--|---|---|---|
| 10 | | $x \geq -1$ oe $x + y \leq 4$ oe $y \geq \frac{1}{3}x - 2$ oe | 3 | B3 for all 3 correct inequalities (B2 for two correct inequalities B1 for one correct inequality) (SC B3 for $x \leq -1$, $x + y \geq 4$ and $y \leq \frac{1}{3}x - 2$ oe) (If no marks gained B1 for understanding of equation $x + y = 4$ e.g. $y > 4 - x$) Accept $<$ for \leq and $>$ for \geq throughout |
| | | | | Total 3 marks |

| | | | | |
|-----------|--|---|-----|--|
| 11 | | $6000 \times 1.015^2 (= 6181.35)$ or $6000 + (0.015 \times 6000) + (0.015 \times (6000 +$ '90')) (= 6181.35) or $(1.015)^2 (= 1.030225)$ or $\frac{6311.16}{6000} (= 1.05186)$ | 3 | M1 for working out the total amount after two years or working out the compound interest multiplier after two years or working out the compound interest multiplier after three years |
| | | $6311.16 \div '6181.35' (= 1.021) (\times 100)$ or $\frac{6311.16 - '6181.35'}{'6181.35'} (= 1.021) (\times 100)$ or '1.05186' \div '1.030225' (= 1.021) ($\times 100$) | | M1 (dep on M1) for a complete method to find the compound interest multiplier ($\times 100$) |
| | | | 2.1 | A1 awrt 2.1 |
| | | | | Total 3 marks |

| | | | | | |
|----------------------|-----|---------------|----|---|--|
| 12 | (a) | E.g. 56 – 38 | | 2 | M1 for subtracting readings from 60 and 20 oe |
| | | | 18 | | A1 for answer in the range 17 – 19 |
| | (b) | [40.5, 43] | | 3 | B1 |
| | | '42' ÷ 0.6 oe | | | M1 for complete method to find the number of men |
| | | | 70 | | A1 |
| Total 5 marks | | | | | |

| | | | | | |
|----------------------|--|---|------|---|--|
| 13 | | $0.14 = \frac{56}{w^2}$ oe or $56 \div 0.14 (= 400)$ | | 4 | M1 for using the given formula correctly |
| | | $\sqrt{\frac{56}{0.14}}$ or $\sqrt{400}$ (=20) | | | M1 for a method to find w |
| | | '20' × '20' × '20' oe | | | M1 (dep on M2) for a method to find the volume of the cube |
| | | | 8000 | | A1 |
| Total 4 marks | | | | | |

| | | | | | |
|----------------------|-----|--|------|---|--|
| 14 | (a) | $(0.5 \times) 9.3 \times 14.7 \times \sin 106$ or $(9.3 \times \cos 16) \times 14.7$ or $(9.3 \times \sin 74) \times 14.7$ | | 2 | M1 for applying the area of a triangle formula using correct values (to find half of the area of the parallelogram) or for a correct method to find the area of the parallelogram |
| | | | 131 | | A1 awrt 131 |
| | (b) | $(GE^2 =) 9.3^2 + 14.7^2 - 2 \times 9.3 \times 14.7 \times \cos 106$ | | 3 | M1 for the correct use of the cosine rule |
| | | 377(.9....) or 378 or $86.49 + 216.09 + 75.3...$ or $302.58 + 75.3....$ | | | M1 (dep on M1) for the correct order of operations |
| | | | 19.4 | | A1 for 19.4 – 19.5 |
| Total 5 marks | | | | | |

| | | | | | | |
|----|-----|---|-------|---|--|---|
| 15 | (a) | $(2x + 5)(x + 1) = 2x^2 + 2x + 5x + 5$ $(= 2x^2 + 7x + 5)$ or $(x + 1)(3 - x) = -x^2 + 3x - x + 3$ $(= -x^2 + 2x + 3)$ or $(3 - x)(2x + 5) = -2x^2 + 6x - 5x + 15$ $(= -2x^2 + x + 15)$ | | 3 | M1 for multiplying out two brackets correctly at least 3 terms correct | M2 for at least 4 terms correct out of a maximum of 8 terms $6x^2 - 2x^3 + 6x - 2x^2 + 15x - 5x^2 + 15 - 5x$ |
| | | E.g. $[(2x^2 + 7x + 5)(3 - x) =]$ $-2x^3 - 7x^2 - 5x + 6x^2 + 21x + 15$ or $[(-x^2 + 2x + 3)(2x + 5) =]$ $-2x^3 - 5x^2 + 10x + 4x^2 + 6x + 15$ or $[(-2x^2 + x + 15)(x + 1) =]$ $-2x^3 - 2x^2 + 15x + x^2 + x + 15$ | | | M1 for at least 3 terms correct out of a maximum of 6 terms or for at least 4 terms correct out of a maximum of 8 terms | |
| | | | Shown | | A1 | |

| | | | | | |
|----|-----|---|------|---|--|
| 15 | (b) | $\left(\frac{dV}{dx} =\right) 16 - 2x + (3 \times -2x^2)$ oe | | 5 | M1 for the correct differentiation of at least 2 correct terms from 16 or $-2x$ or $(3 \times -2x^2)$ |
| | | $\left(\frac{dV}{dx} =\right) 16 - 2x - 6x^2$ oe | | | A1 for a correct differentiated expression |
| | | ' $16 - 2x - 6x^2 = 0$ ' oe | | | M1 (dep on M1) for equating their differentiated expression to zero |
| | | E.g. $(x =) \frac{-2 \pm \sqrt{2^2 - 4 \times 6 \times -16}}{2 \times 6}$ oe (accept + in place of \pm) or E.g. $6 \left(\left(x + \frac{1}{6} \right)^2 - \left(\frac{1}{6} \right)^2 \right) - 16 (= 0)$ oe | | | M1 (dep on M1) for a complete method to solve their 3-term quadratic equation (allow one sign error and some simplification – allow as far as $\frac{-2 \pm \sqrt{4 + 384}}{12}$) |
| | | | 1.47 | | A1 dep on M1 for answer in range 1.47 – 1.5 from correct working (Must reject -1.80 to -1.81 if calculated) |
| | | | | | Total 8 marks |

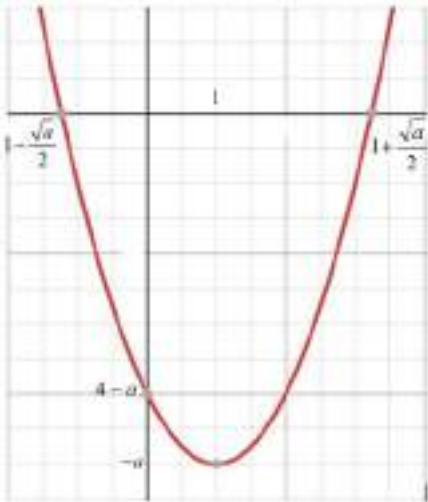
| | | | | | |
|----|--|--|-------|---|---|
| 16 | | 58.35 or 58.45 or 19.5 or 20.5 or 3.55 or 3.65 | | 3 | B1 for any correct bound Accept $58.44\dot{9}$ for 58.45 or $20.4\dot{9}$ for 20.5 or $3.64\dot{9}$ for 3.65 |
| | | $\frac{2 \times 58.45 - 19.5}{3.55}$ (= 27.4366...) | | | M1 for correct substitution into $\frac{2 \times a_{UB} - c_{LB}}{d_{LB}}$ where $58.4 < a_{UB} \leq 58.45$ and $19.5 \leq c_{LB} < 20$ and $3.55 \leq d_{LB} < 3.6$ |
| | | | 27.44 | | A1 from correct working allow 27.4 – 27.5 |
| | | | | | Total 3 marks |

| | | | | | |
|----|-----|---|-------|---|--|
| 17 | (a) | $6 \times 6 + 6 \times 2\sqrt{12} + 6 \times 2\sqrt{12} + (2 \times \sqrt{12})^2$ or $36 + 12\sqrt{12} + 12\sqrt{12} + 4\sqrt{12}\sqrt{12}$ or $36 + 12\sqrt{12} + 12\sqrt{12} + (4 \times 12)$ or $36 + 24\sqrt{3} + 24\sqrt{3} + 48$ or $36 + 2 \times 24\sqrt{3} + 48$ or $36 + 6 \times 2 \times 2\sqrt{12} + 48$ | | 3 | M1 for correct expansion of brackets showing four terms (need not be simplified) or for the use of $(a + b)^2 = a^2 + 2ab + b^2$ or for showing or stating $\sqrt{12} = 2\sqrt{3}$ oe |
| | | $84 + 48\sqrt{3}$ | | | M1 (dep on M1) |
| | | | Shown | | A1 for fully correct working leading to given expression |

| | | | | | |
|----------------------|-----|--|-----------------------|---|---|
| 17 | (b) | E.g. $\left(\frac{3a^4}{t^5}\right)^{-2}$ or $\left(\frac{t^{15}}{27a^{12}}\right)^{\frac{2}{3}}$ or $\left(\frac{729a^{24}}{t^{30}}\right)^{-\frac{1}{3}}$ | | 3 | M1 for one of cube rooting or inverting or squaring or $\frac{ka^{-8}}{t^{-10}}$ where k is an integer $\neq 0$ |
| | | E.g. $\left(\frac{9a^8}{t^{10}}\right)^{-1}$ or $\frac{3^{-2}a^{-8}}{t^{-10}}$ or $\frac{1}{9}a^{-8}$ or $\left(\frac{t^5}{3a^4}\right)^2$ or $\left(\frac{t^{30}}{729a^{24}}\right)^{\frac{1}{3}}$ or $\frac{a^{-8}}{9t^{-10}}$ | | | M1 for two of cube rooting or inverting or squaring or $\frac{t^{10}}{ka^8}$ where k is an integer $\neq 0$ |
| | | | $\frac{t^{10}}{9a^8}$ | | A1 Allow $\frac{t^{10}a^{-8}}{9}$ or $\frac{1}{9}t^{10}a^{-8}$ |
| Total 6 marks | | | | | |

| | | | | | |
|----|--|--------------------|---|---|---|
| 18 | $\frac{4}{16} \times \frac{3}{15} \times \frac{2}{14} \left(= \frac{24}{3360} = \frac{1}{140} \right) \text{ oe or } \frac{7}{16} \times \frac{6}{15} \times \frac{5}{14} \left(= \frac{210}{3360} = \frac{1}{16} \right) \text{ oe or}$ $\frac{5}{16} \times \frac{4}{15} \times \frac{3}{14} \left(= \frac{60}{3360} = \frac{1}{56} \right) \text{ oe}$ | | 4 | M1 for finding <i>BBB or OOO</i> or <i>LLL</i> | M3 for $\frac{11}{16} \times \frac{10}{15} \times \frac{9}{14} \text{ oe}$ |
| | $\frac{4}{16} \times \frac{7}{15} \times \frac{6}{14} \left(= \frac{168}{3360} = \frac{1}{20} \right) \text{ oe or } \frac{4}{16} \times \frac{3}{15} \times \frac{7}{14} \left(= \frac{84}{3360} = \frac{1}{40} \right) \text{ oe}$ or $\frac{5}{16} \times \frac{4}{15} \times \frac{4}{14} \left(= \frac{80}{3360} = \frac{1}{42} \right) \text{ oe or } \frac{5}{16} \times \frac{4}{15} \times \frac{7}{14} \left(= \frac{140}{3360} = \frac{1}{24} \right) \text{ oe or}$ $\frac{5}{16} \times \frac{4}{15} \times \frac{3}{14} \left(= \frac{60}{3360} = \frac{1}{56} \right) \text{ oe or } \frac{5}{16} \times \frac{7}{15} \times \frac{6}{14} \left(= \frac{210}{3360} = \frac{1}{16} \right) \text{ oe or}$ $\frac{5}{16} \times \frac{7}{15} \times \frac{4}{14} \left(= \frac{140}{3360} = \frac{1}{24} \right) \text{ oe}$ or $\frac{5}{16} \times \frac{4}{15} \times \frac{11}{14} \left(= \frac{220}{3360} = \frac{11}{168} \right) \text{ oe or } \frac{5}{16} \times \frac{11}{15} \times \frac{10}{14} \left(= \frac{550}{3360} = \frac{55}{336} \right) \text{ oe}$ | | | M1 for finding the following in any order <i>BOO or BBO</i> or <i>LLB or LLO or LBB or LOO</i> or <i>LOB</i> or <i>LLX or LXX (X = not L)</i> | |
| | $, \frac{24}{3360} , + 3 \times , \frac{84}{3360} , + , \frac{210}{3360} , + 3 \times , \frac{168}{3360} , \text{ oe or}$ $1 - \left(, \frac{60}{3360} , + 3 \times , \frac{80}{3360} , + 3 \times , \frac{140}{3360} , + 3 \times , \frac{60}{3360} , 3 \times , \frac{210}{3360} , 6 \times , \frac{140}{3360} , \right) \text{ oe or}$ $1 - \left(, \frac{60}{3360} , + 3 \times , \frac{220}{3360} , + 3 \times , \frac{550}{3360} , \right) \text{ oe}$ | | | M1 for a complete method | |
| | | $\frac{990}{3360}$ | | A1 for $\frac{990}{3360}$ oe e.g. $\frac{33}{112}$ or 0.29(464...) | |
| | | | | | Total 4 marks |

| | | | | |
|----------------------|---|------|---|--|
| 19 | $(AH =) \sqrt{6^2 + 5^2 + 9^2} (= \sqrt{142})$ or $(FH = GE =) \sqrt{5^2 + 9^2} (= \sqrt{106})$ | | 4 | M1 for working out AH or FH or GE |
| | E.g. $\sin AHF = \frac{6}{\sqrt{142}}$ or $\tan AHF = \frac{6}{\sqrt{106}}$ or $\cos AHF = \frac{\sqrt{106}}{\sqrt{142}}$ or $\sin FAH = \frac{\sqrt{106}}{\sqrt{142}}$ or $\cos FAH = \frac{6}{\sqrt{142}}$ or $\tan FAH = \frac{\sqrt{106}}{6}$ | | | M1 for a correct method for finding angle AHF or finding angle FAH Allow $\cos AHF = \left(\frac{\sqrt{142}^2 + \sqrt{106}^2 - 6^2}{2 \times \sqrt{142} \times \sqrt{106}} \right)$ oe or $\sin AHF = \frac{\sin 90}{\sqrt{142}} \times 6$ oe |
| | E.g. $\sin^{-1} \left(\frac{6}{\sqrt{142}} \right)$ or $\tan^{-1} \left(\frac{6}{\sqrt{106}} \right)$ or $\cos^{-1} \left(\frac{\sqrt{106}}{\sqrt{142}} \right)$ or $90 - \sin^{-1} \left(\frac{\sqrt{106}}{\sqrt{142}} \right)$ or $90 - \cos^{-1} \left(\frac{6}{\sqrt{142}} \right)$ or $90 - \tan^{-1} \left(\frac{\sqrt{106}}{6} \right)$ | | | M1 for a complete method Allow $\cos^{-1} \left(\frac{\sqrt{142}^2 + \sqrt{106}^2 - 6^2}{2 \times \sqrt{142} \times \sqrt{106}} \right)$ oe or $\sin^{-1} \left(\frac{\sin 90}{\sqrt{142}} \times 6 \right)$ oe |
| | | 30.2 | | A1 for 30.2 – 30.3 |
| Total 4 marks | | | | |

| | | | | |
|----|--|---------------|---|--|
| 20 | graph drawn in shape of a quadratic with a minimum in any quadrant | | 4 | M1 for a quadratic with a minimum |
| | $x = 1, y = 4(1 - 1)^2 - a$ | | | M1 for finding the turning point (may be seen marked on the graph as $(1, -a)$) |
| | $x = 1 \pm \sqrt{\frac{a}{4}}$ oe or $y = 4 - a$ | | | M1 for finding one of the intercepts (or award for any one correct coordinate shown on graph) $(0, 4 - a)$ or $(1 + \frac{\sqrt{a}}{2}, 0)$ or $(1 - \frac{\sqrt{a}}{2}, 0)$ Note: The 0's can be ignored (as shown in the diagram) |
| |  | Correct graph | | A1 for a fully correct graph <ul style="list-style-type: none"> quadratic shape with minimum in the fourth quadrant and marked as $(1, -a)$ oe x-axis intercepts marked as $(1 + \frac{\sqrt{a}}{2}, 0)$ oe on the positive x-axis and $(1 - \frac{\sqrt{a}}{2}, 0)$ oe on the negative x-axis y-axis intercept marked as $(0, 4 - a)$ oe Note: The 0's can be ignored (as shown in the diagram) |
| | | | | |
| | | | | Total 4 marks |

| | | | | |
|----------------------|---|---------------------|---|---|
| 21 | (fg(x) =) $(x + 3)^2 - 2(x + 3)$ oe | | 5 | M1 for substituting $g(x)$ into $f(x)$ |
| | (fg(x) =) $x^2 + 4x + 3$ | | | A1 Allow $y^2 + 4y + 3$ |
| | $(x + 2)^2 - 4 + 3$ or $(x + 2)^2 - 1$ or $x^2 + 4x + (3 - y) = 0$ or $y^2 + 4y + (3 - x) = 0$ | | | M1 ft (dep on M1) for correctly completing the square on their 3 term quadratic or Correctly setting up an equation |
| | $(x + 2)^2 = y + 1$ or $(y + 2)^2 = x + 1$ or $x = \frac{-4 \pm \sqrt{16 - 4(3 - y)}}{2}$ or $x = -2 \pm \sqrt{1 + y}$ | | | M1 ft (dep on M2) for a correct rearrangement for their completed the square quadratic or correctly substituting into the quadratic formula Allow same equations with x and y swapped |
| | | $-2 + \sqrt{x + 1}$ | | A1 oe |
| Total 5 marks | | | | |

| | | | | |
|----|--|--|---|--|
| 22 | gradient of $JK = -0.5$ or $m \times 2 = -1$ | | 6 | M1 for finding the gradient of JK using $m_1 \times m_2 = -1$ |
| | $\frac{k-15}{6-j} = -\frac{1}{2}$ or $2k-j = 24$ or $j = 2k-24$ or $k = \frac{j+24}{2}$ oe | | | M1 for expressing the gradient of JK in terms of j and k or a correct equivalent equation |
| | $(j-6)^2 + (k-15)^2 = 80$ oe or $\left(\frac{j+6}{2}, \frac{k+15}{2}\right)$ oe or $(j+4)^2 + 196 = 100 + (k-1)^2$ oe | | | M1 for finding equation of JK in terms of j and k or for finding the midpoint of M or for equating length HJ with length HK |
| | eg $3k^2 - 78k + 495 = 0$ oe or $5j^2 - 60j - 140 = 0$ oe or $5k^2 - 150k + 1045 = 0$ oe or $3j^2 - 12j - 36 = 0$ oe or gradient HM : eg $\frac{\frac{k+15}{2}-1}{\frac{j+6}{2}+4} = 2$ or $k = 2j + 15$ or $j = \frac{k-15}{2}$ oe | | | M1 (dep on M3) writing a correct quadratic expression in the form $ax^2 + bx + c (= 0)$ (allow $ax^2 + bx = c$) or A correct equation for the gradient of HM in terms of j and k or a correct equivalent equation |
| | eg $(k-15)(k-11)(=0)$ or $\frac{78 \pm \sqrt{(-78)^2 - 4 \times 3 \times 495}}{2 \times 3}$ or $(k-13)^2 - 169 + 165 (=0)$ | eg $(j-6)(j+2)(=0)$ or $\frac{12 \pm \sqrt{(-12)^2 - 4 \times 3 \times -36}}{2 \times 3}$ or $(j-2)^2 - 4 - 12 (=0)$ | | M1 (dep on M3) for a complete method to solve their 3-term quadratic equation (allow one sign error in the use of the quadratic formula) or a correct method to eliminate either j or k eg $2k - 24 = \frac{k-15}{2}$ oe or $\frac{j+24}{2} = 2j + 15$ oe |
| | $j = -2, k = 11$ | | | A1 |
| | | | | Total 6 marks |

| | | | | | |
|------------|--|---|--|---|--|
| 22 | | $\left(\frac{j+6}{2}, \frac{k+15}{2}\right)$ oe | | 6 | M1 for finding the midpoint of M |
| ALT | | $\frac{\frac{k+15}{2}-1}{\frac{j+6}{2}+4} = 2$ or $k - 2j = 15$ or $k = 2j + 15$ or $j = \frac{k-15}{2}$ oe | | | M1 for expressing the gradient of JK in terms of j and k or a correct equivalent equation |
| | | $(j-6)^2 + (k-15)^2 = 80$ oe or $(j+4)^2 + 196 = 100 + (k-1)^2$ oe | | | M1 for finding the length of JK in terms of j and k or for equating length HJ with length HK |
| | | E.g. $5j^2 - 12j - 44 = 0$ or $3j^2 + 48j + 84 = 0$ oe | E.g. $5k^2 - 174k + 1309 = 0$ or $3k^2 + 6k - 429 = 0$ oe | | M1 (dep on M3) writing the correct quadratic expression in form $ax^2 + bx + c (= 0)$ allow $ax^2 + bx = c$ |
| | | E.g. $(5j - 22)(j + 2) (= 0)$ or $\frac{12 \pm \sqrt{(-12)^2 - 4 \times 5 \times -44}}{2 \times 5}$ or $(j + 8)^2 - 64 + 28 (= 0)$ | E.g. $(5k - 119)(k - 11) (= 0)$ or $\frac{174 \pm \sqrt{(-174)^2 - 4 \times 5 \times 1309}}{2 \times 5}$ or $(k + 1)^2 - 1 - 143 (= 0)$ | | M1 (dep on M3) for a complete method to solve their 3-term quadratic equation (allow one sign error in the use of the quadratic formula) |
| | | $j = -2, k = 11$ | | | A1 |
| | | | | | Total 6 marks |