

Answer ALL TWENTY FIVE questions.

Write your answers in the spaces provided.

You must write down all the stages in your working.

1 Here are the first four terms of an arithmetic sequence.

1 4 7 10 +3

(a) Find an expression, in terms of n , for the n th term of this sequence.

3 6 9 12

$3n - 2$

(2)

The n th term of a different arithmetic sequence is $5n + 17$

(b) Find the 12th term of this sequence.

$5 \times 12 + 17$

77

(1)

(Total for Question 1 is 3 marks)



P 7 3 9 9 0 A 0 3 2 8

2 450 students were asked how they travelled to school on Monday.
Each student walked or travelled by bus or travelled by car or travelled by bicycle.
Each student used just one method of travel.

One of these students is chosen at random.

The table shows information about the probability of each method of travel.

Method of travel	walk	bus	car	bicycle
Probability	0.20	x	$2x$	0.26

Work out how many of the 450 students travelled by car.

$$\begin{aligned}3x + 0.46 &= 1 \\3x &= 0.54 \\x &= 0.18\end{aligned}$$

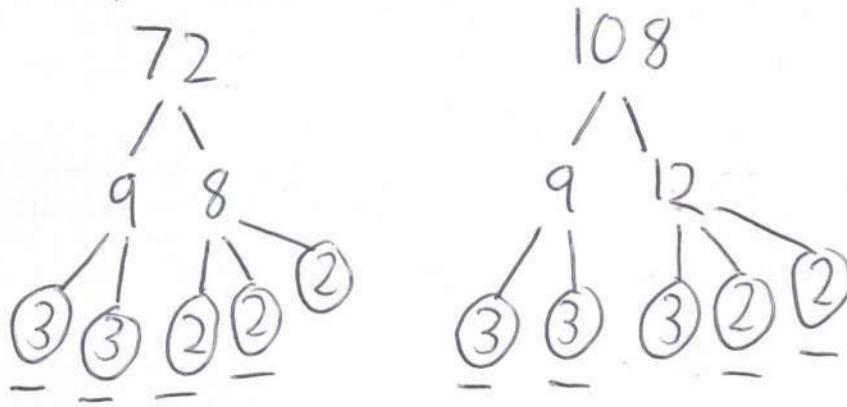
$$\text{Car} = 450 \times (2 \times 0.18)$$

$$450 \times 0.36 = 162$$

(Total for Question 2 is 4 marks)



3 Find the highest common factor (HCF) of 72 and 108
Show your working clearly.



$$\text{HCF} = 3 \times 3 \times 2 \times 2 = 36$$

(Total for Question 3 is 2 marks)

4 Ava records the number of kilometres she drives each month.

In April, Ava drove 943 kilometres.

This is 15% more than the number of kilometres she drove in March.

Work out the number of kilometres Ava drove in March.

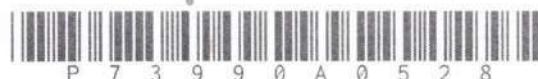
$$? \times 1.15 = 943$$

$$943 \div 1.15$$

820

.....kilometres

(Total for Question 4 is 3 marks)



5 In the diagram, $ABCDE$ is a regular pentagon.

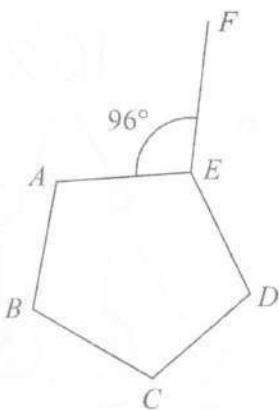


Diagram NOT
accurately drawn

Angle $AEF = 96^\circ$

Work out the size of the obtuse angle FED
Show your working clearly.

$$\text{Internal} = \frac{(5-2) \times 180}{5} = 108$$

$$\angle FED = 360 - 108 - 96$$

156

(Total for Question 5 is 4 marks)



6 (a) Expand and simplify $(m + 5)(m - 8)$

$$= m^2 - 8m + 5m - 40$$

$$= m^2 - 3m - 40$$

(2)

(b) Solve $3n - 4 = \frac{5n + 6}{3}$

(x3)

Show clear algebraic working.

$$9n - 12 = 5n + 6$$

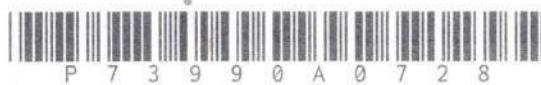
$$4n = 18$$

$$n = \frac{18}{4} \quad \therefore \quad n = \frac{9}{2}$$

$$n = 4.5$$

(3)

(Total for Question 6 is 5 marks)



7 $E = \{23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34\}$
 $A = \{\text{even numbers}\}$
 $B = \{23, 29, 31\}$
 $C = \{\text{multiples of 3}\}$

(a) List the members of the set

(i) $B \cup C$

23, 24, 27, 29, 30, 31, 33
(1)

(ii) $A' \cap C$

27, 33
(1)

(b) Is it true that $B \cap C = \emptyset$?

Tick (\checkmark) one of the boxes below.

Yes

No

Give a reason for your answer.

No multiples of 3 in set B

(1)

The set D has 4 members and is such that $D \cap (A \cup C) = \emptyset$

(c) List the members of set D

23, 25, 29, 31
(2)

(Total for Question 7 is 5 marks)



8 A cylinder is placed on a table.

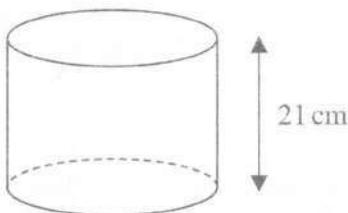


Diagram NOT
accurately drawn

The volume of the cylinder is 1575 cm^3

The force exerted by the cylinder on the table is 84 newtons.

$$\text{pressure} = \frac{\text{force}}{\text{area}}$$

Work out the pressure on the table due to the cylinder.

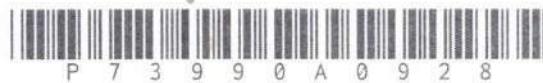
$$\text{Base area} = \frac{1575}{21} = 75$$

$$P = \frac{84}{75} = \frac{28}{25}$$

1.12

newtons/cm²

(Total for Question 8 is 3 marks)



9 The table gives the amount of rice produced by each of two countries in 2020

Country	Amount of rice (tonnes)
Indonesia	3.5×10^7
Argentina	8.2×10^5

(a) Write 3.5×10^7 as an ordinary number.

35 000 000

(1)

In 2020, Japan produced 6 780 000 more tonnes of rice than Argentina.

(b) Work out the amount of rice Japan produced in 2020
Give your answer in standard form.

$$8.2 \times 10^5 + 6780000$$

$$= 7600000$$

7.6 $\times 10^6$

tonnes

(2)

(Total for Question 9 is 3 marks)



10 (a) Simplify $(2p)^0$ where $p > 0$

(1)

$$y^9 \times y^{-3} = y^n$$

(b) Find the value of n

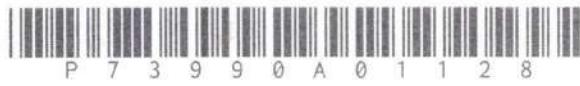
6
(1)

(c) Simplify fully $(5a^4c^2)^3$

$$125a^{12}c^6$$

(2)

(Total for Question 10 is 4 marks)



11 The diagram shows a roof support.

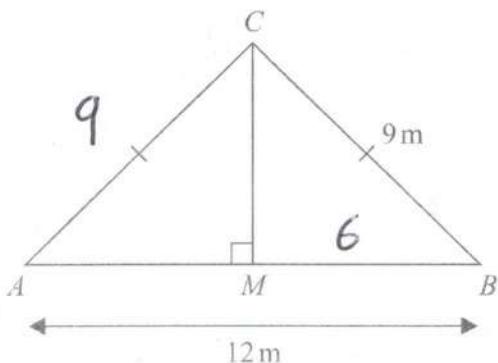


Diagram NOT
accurately drawn

The roof support is made from four lengths of wood, AB , AC , BC and MC

$$AC = BC = 9 \text{ m} \quad AB = 12 \text{ m}$$

$$\text{angle } AMC = 90^\circ$$

Lewis is going to buy lengths of wood to make the roof support.

The wood costs 21.50 euros per metre.

Each length of wood he buys has to be a whole number of metres.

Work out the total cost of the wood Lewis needs to buy.

Show your working clearly.

$$CM = \sqrt{9^2 - 6^2} = \sqrt{45}$$

$$9+9+12+\sqrt{45} = 36.7...$$

= 37 lengths

$$37 \times 21.5 = 795.50$$

euros

(Total for Question 11 is 4 marks)



12 (a) Factorise fully $6y^2 - 5y - 4$

$$ac = -24$$

$$\begin{array}{c} 6y^2 + 3y \quad | -8y \quad -4 \\ 3y(2y+1) \quad | -4(2y+1) \end{array}$$

$$(2y+1)(3y-4)$$

(2)

(b) Express $\frac{2x+1}{4x} + \frac{7-5x}{3x}$ as a single fraction in its simplest form.

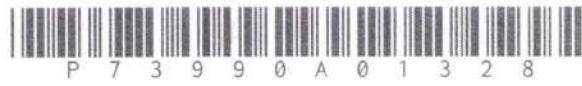
$$\frac{3(2x+1) + 4(7-5x)}{12x}$$

$$\frac{6x+3 + 28-20x}{12x}$$

$$\frac{-14x + 31}{12x}$$

(3)

(Total for Question 12 is 5 marks)

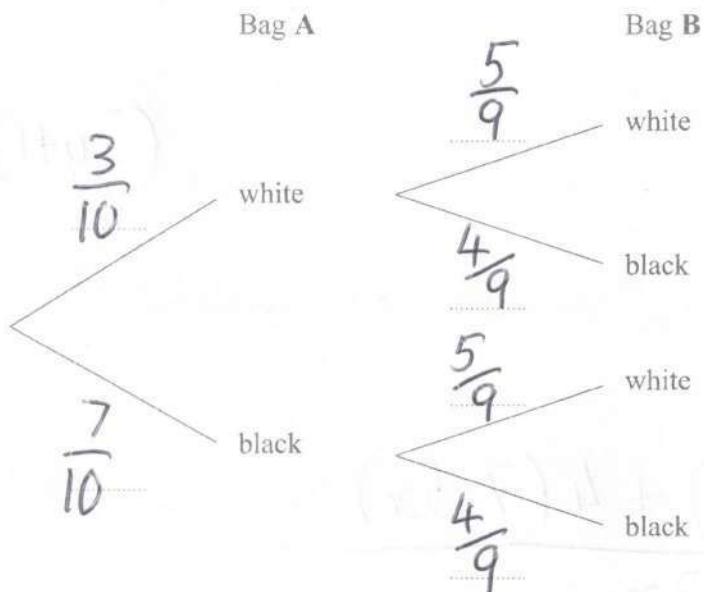


13 Harman has two bags of beads.

In bag A, there are 3 white beads and 7 black beads.
In bag B, there are 5 white beads and 4 black beads.

Harman takes at random a bead from bag A and a bead from bag B

(a) Complete the probability tree diagram.



(2)

(b) Work out the probability that Harman takes two beads of the same colour.

$$\begin{aligned}
 &= WW + BB \\
 &= \left(\frac{3}{10} \times \frac{5}{9}\right) + \left(\frac{7}{10} \times \frac{4}{9}\right) = \frac{43}{90}
 \end{aligned}$$

(3)

(Total for Question 13 is 5 marks)



14 The combined savings of Abel and Bahira are 15435 dinars.

The savings of Bahira are 45% more than the savings of Abel.

The savings of Bahira are $\frac{3}{2}$ times the savings of Chanda.

Work out the savings of Chanda.

$$\begin{array}{ccc} A & B & C \\ 100x & 145x & \\ \underbrace{\quad\quad\quad}_{15435} \end{array}$$

$$245x = 15435$$

$$x = 63$$

$$B = 145 \times 63 = 9135$$

$$C = 9135 \div \frac{3}{2} = 6090$$

..... dinars

(Total for Question 14 is 5 marks)



15 The function f is defined as

$$f: x \mapsto \frac{3x+1}{x-2}$$

(a) State the value of x that cannot be included in any domain of the function f .

$$x-2 \neq 0$$

2

(1)

(b) Express the inverse function f^{-1} in the form $f^{-1}(x) = \dots$

$$y = \frac{3x+1}{x-2}$$

$$y(x-2) = 3x+1$$

$$yx-2y = 3x+1$$

$$yx-3x = 1+2y$$

$$x(y-3) = 1+2y$$

$$x = \frac{1+2y}{y-3}$$

$$f^{-1}(x) = \frac{1+2x}{x-3}$$

(3)

(Total for Question 15 is 4 marks)



16 There are 20 sweets in a box.

15 of the sweets are red

5 of the sweets are yellow

Fred takes at random 3 sweets from the box.

Work out the probability that Fred takes at least one sweet of each colour from the box.

R
15

Y
5

$$\begin{aligned}
 P(\geq 1 \text{ each}) &= P(1R, 2Y + 2R, 1Y) \\
 &= 1 - P(3 \text{ same}) \\
 &= 1 - \left(\frac{15 \times 14 \times 13}{20 \times 19 \times 18} \right) - \left(\frac{5 \times 4 \times 3}{20 \times 19 \times 18} \right)
 \end{aligned}$$

$$= 1 - \frac{2790}{6840}$$

$$\frac{45}{76}$$

(Total for Question 16 is 4 marks)

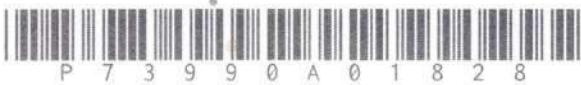


17 Show that $\frac{1+\sqrt{5}}{3-\sqrt{5}}$ can be written in the form $a + \sqrt{b}$ where a and b are integers.

Show each stage of your working clearly.

$$\begin{aligned}\frac{1+\sqrt{5}}{3-\sqrt{5}} \times \frac{3+\sqrt{5}}{3+\sqrt{5}} &= \frac{3+\sqrt{5} + 3\sqrt{5} + 5}{9-5} \\ &= \frac{8 + 4\sqrt{5}}{4} \\ &= 2 + \sqrt{5}\end{aligned}$$

(Total for Question 17 is 3 marks)



18 A curve C has equation $y = x^3 - 40x + 1$

Find the coordinates of both the points on C at which the gradient is 8

$$\frac{dy}{dx} = 3x^2 - 40 = 8$$

$$3x^2 = 48$$

$$x^2 = 16$$

$$x = 4$$

$$y = 4^3 - 40 \times 4 + 1$$

$$= -95$$

$$x = -4$$

$$y = (-4)^3 - 40 \times (-4) + 1$$

$$= 97$$

$$\begin{array}{c} 4 \quad -95 \\ (-, \quad ,) \\ -4 \quad 97 \end{array}$$

(Total for Question 18 is 5 marks)



19 Here is quadrilateral $ABCD$

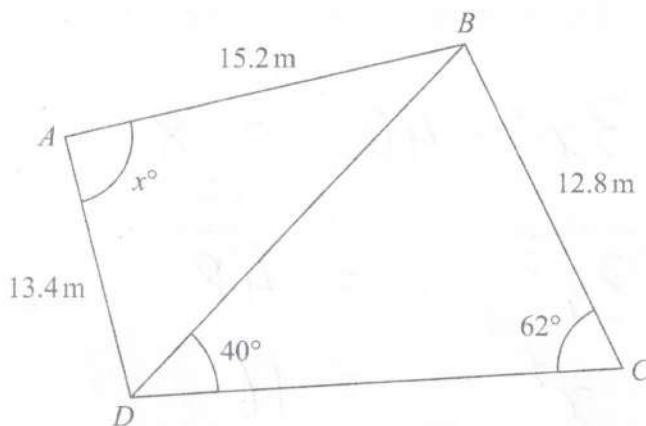


Diagram NOT
accurately drawn

Work out the value of x .
Give your answer correct to 3 significant figures.

$$\frac{BD}{\sin 62} = \frac{12.8}{\sin 40} \quad BD = 17.58\ldots$$

$$BD^2 = 13.4^2 + 15.2^2 - 2 \times 13.4 \times 15.2 \times \cos x$$

$$\cos x = 0.2490\ldots$$

$$x = \cos^{-1}(0.249) = 75.577\ldots$$

$$x = 75.6$$

(Total for Question 19 is 5 marks)



20 The diagram shows a sector $OABC$ of a circle centre O

$$\frac{60}{360} = \frac{1}{6}$$

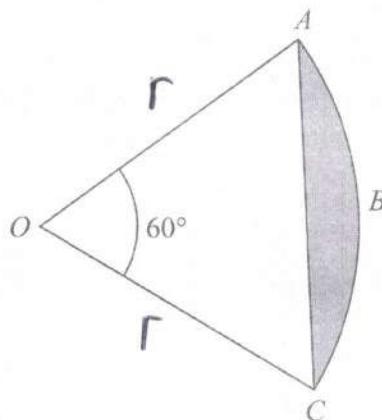


Diagram NOT accurately drawn

Angle $AOC = 60^\circ$

The area of the shaded segment ABC is 38 cm^2

Work out the perimeter of the shaded segment ABC
Give your answer correct to one decimal place.

$$\text{Area sector} = \pi r^2 \times \frac{1}{6}$$

$$\text{Area triangle} = \frac{1}{2} \times r \times r \times \sin 60 = \frac{r^2 \sqrt{3}}{4}$$

$$\text{so } 38 = \frac{\pi r^2}{6} - \frac{r^2 \sqrt{3}}{4}$$

$$r = \sqrt{\frac{38}{\frac{\pi}{6} - \frac{\sqrt{3}}{4}}} = 20.48\dots$$

$$AC = \sqrt{(2 \times 20.48^2) - 2 \times 20.48 \cos 60}$$

$$\text{Per} = \frac{2 \times \pi \times 20.48}{6} + 20.48$$

(41.9)

cm

(Total for Question 20 is 4 marks)

$$(AC^2 = 20.48^2 + 20.48^2 - 2 \times 20.48 \cos 60)$$



P 7 3 9 9 0 A 0 2 1 2 8

21 A curve has equation $y = f(x)$

There is one minimum point on this curve.

The coordinates of this minimum point are $(5, -4)$

Write down the coordinates of the minimum point on the curve with equation

(i) $y = f(x + 7)$

$\leftarrow 7$

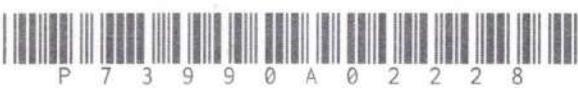
$(-2, -4)$
(1)

(ii) $y = f(x) - 6$

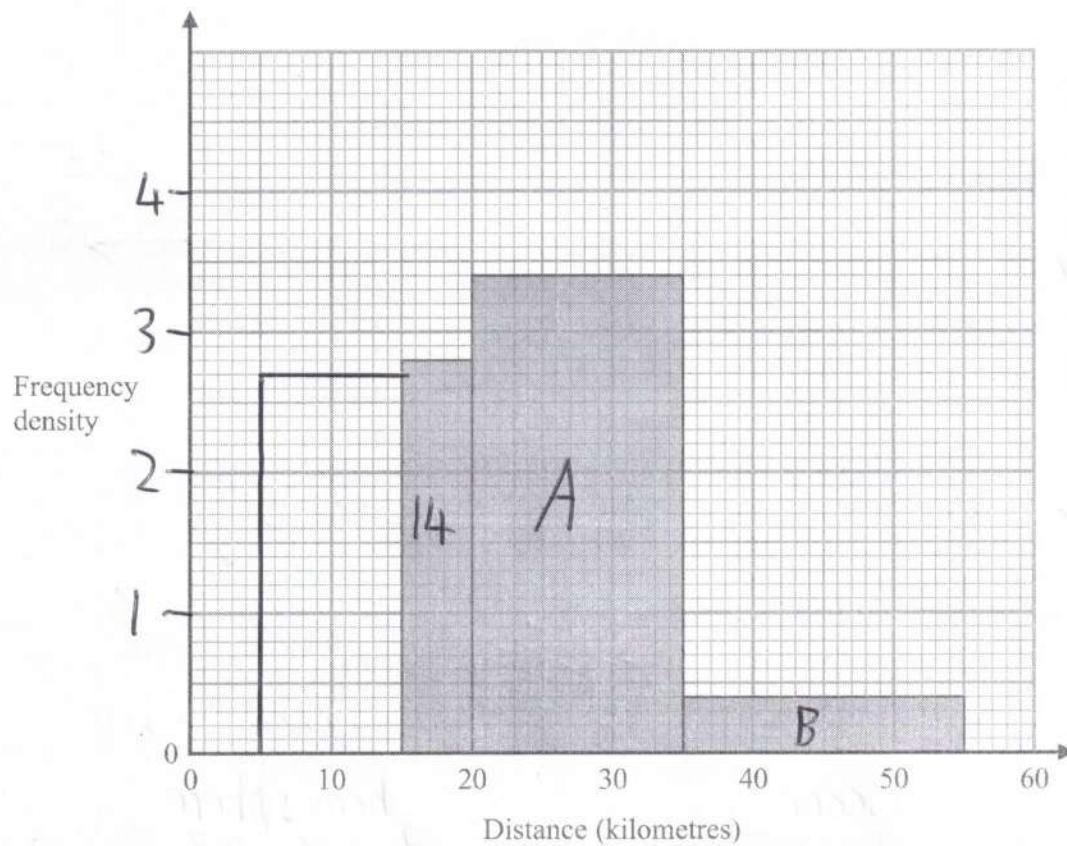
$\downarrow 6$

$(5, -10)$
(1)

(Total for Question 21 is 2 marks)



22 The incomplete histogram shows some information about the distances, in kilometres, that 100 adults ran last week.



All of the adults ran at least 5 kilometres.

None of the adults ran more than 55 kilometres.

14 adults ran between 15 kilometres and 20 kilometres.

$$fd = 14 \div 5 = 2.8$$

Complete the histogram.

$$A = 15 \times 3.4 = 51$$

$$B = 20 \times 0.4 = 8$$

$$100 - (8 + 51 + 14) = 27$$

$$\text{so } 5m \rightarrow 15m = 27$$

$$fd = \frac{27}{10} = 2.7$$

(Total for Question 22 is 3 marks)



P 7 3 9 9 0 A 0 2 3 2 8

23 A solid shape is made by removing a hemisphere, shown shaded, from a cone as shown in the diagram.

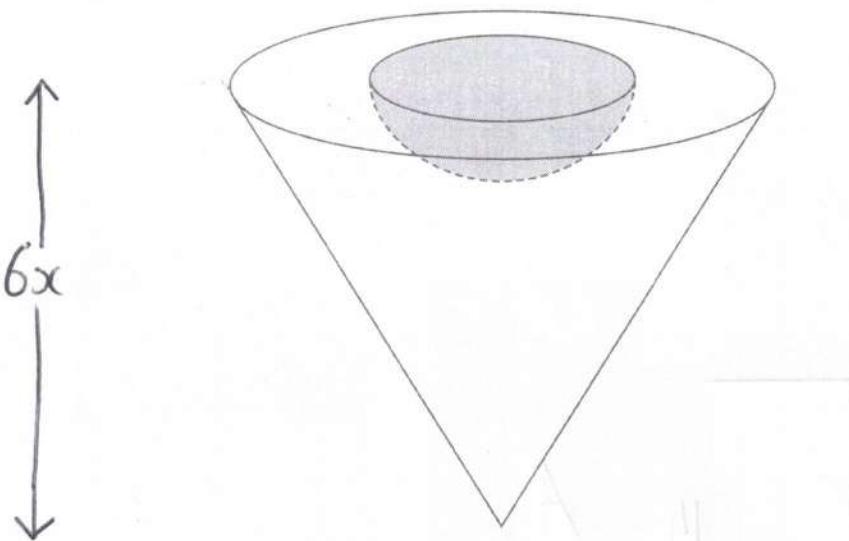


Diagram **NOT**
accurately drawn

The radius of the hemisphere is $2x$ cm

The radius of the base of the cone is $5x$ cm

The vertical height of the cone is $6x$ cm

The volume of the solid shape is $6948\pi \text{ cm}^3$

Work out the **total** surface area of the solid hemisphere that has been removed from the cone.

Give your answer correct to the nearest integer.

$$\begin{aligned}
 6948\pi &= \frac{1}{3}\pi\cancel{x}(5x)^2(6x) - \frac{4}{3}\pi(2x)^3 \div 2 \\
 20844 &= 150x^3 - 16x^3 \\
 x^3 &= 155.552\ldots \quad x = 5.378\ldots
 \end{aligned}$$

$$\begin{aligned}
 \text{SA of hemisphere} &= \pi r^2 + 4\pi r^2 \div 2 \\
 &= (\pi \times 10.756^2) + (2\pi \times 10.756^2) \\
 &= 1090.367\ldots \\
 &= \underline{1090 \text{ cm}^2}
 \end{aligned}$$



24 A polygon has n sides, where $n > 5$

The interior angles of the polygon form an arithmetic sequence.

The smallest angle of the polygon is 84°

The common difference of the sequence is 4°

$$a = 84 \quad d = 4$$

Work out the sum of the interior angles of the polygon.

Show clear algebraic working.

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$\text{Sum of interior} = (n-2) \times 180$$

$$\text{so } 84n + 2n^2 - 2n = 180n - 360$$

$$2n^2 - 98n + 360 = 0$$

$$n^2 - 49n + 180 = 0$$

$$(n-45)(n-4) = 0$$

$$n=4, \text{ reject} \quad \text{so } n=45$$

$$\therefore \text{Sum} = (45-2) \times 180$$

$$= 7740$$



25 $f(x) = 17 - 3x^2 + 12x$

Write $f(x)$ in the form $a - b(x - c)^2$ where a , b and c are constants.

$$-3[x^2 - 4x] + 17$$

$$-3[(x - 2)^2 - 4] + 17$$

$$-3(x-2)^2 + 12 + 17$$

$$f(x) = 29 - 3(x-2)^2$$

(Total for Question 25 is 4 marks)

TOTAL FOR PAPER IS 100 MARKS

