

1. The lengths of the three sides of a triangle are in the ratio 3 : 5 : 7.

(a) What fraction of the perimeter is the longest side of this triangle? [1]

$\frac{7}{15}$ ✓

(b) The perimeter of this triangle is 60 cm.

Find the length of each of the three sides of this triangle. [2]

$60 \div 15 = 4$

3×4

5×4

7×4

12

20

28

cm,

cm,

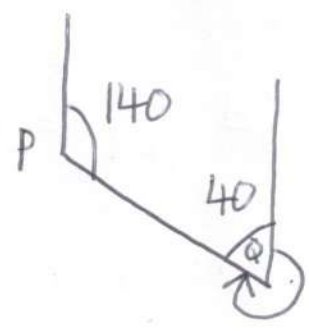
cm

✓
✓

2. The bearing of Q from P is 140° .

(Sketch)

Find the bearing of P from Q. [2]



$360 - 140 = 320^\circ$

✓

✓



3. The n th term of a sequence is given by $2n + 9$.

(a) Work out the difference between consecutive terms. [2]

11, 13 etc ✓

2 ✓

(b) (i) Solve $2n + 9 < 99$. [2]

$$2n < 90 \quad \checkmark$$

$$n < 45 \quad \checkmark$$

(ii) Write down the number of terms of this sequence that are less than 99. [1]

Number of terms =

44 ✓



4. James has been on holiday to the USA and is flying home to the UK.
The price of a gift in a shop at the airport is \$65.
The price of the same gift online is €60 including delivery.

On the day of his flight, the exchange rates were as follows.

$$\begin{aligned} \text{£}0.80 &= \$1 \\ \text{£}1 &= \text{€}1.20 \end{aligned}$$

Is it cheaper to buy the gift at the airport or online?

Airport Online

Show how you decide.

[4]

$$\begin{array}{l} \checkmark \quad \$ \rightarrow \text{£} \\ \quad \quad \times 0.8 \end{array} \quad \begin{array}{r} 65 \\ \times 48 \\ \hline 520 \end{array} \quad \begin{array}{l} \text{(AP)} \\ = \text{£}52 \quad \checkmark \end{array}$$

$$\checkmark \quad \text{€} \rightarrow \text{£} \\ \quad \quad \div 1.2 \quad \begin{array}{r} 50 \\ 12 \overline{)600} \end{array} \quad \begin{array}{l} \text{(On)} \\ = \text{£}50 \quad \checkmark \end{array}$$



5.

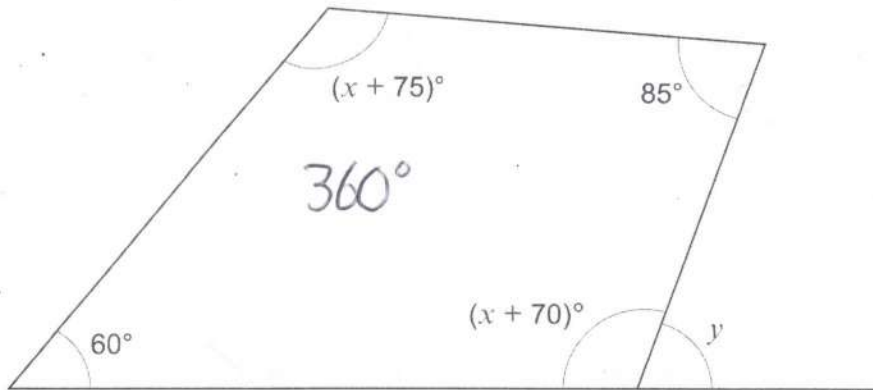


Diagram not drawn to scale

The diagram shows a quadrilateral.

Use algebra to find the size of the exterior angle y .

[5]

$$2x + 290 = 360 \quad \checkmark$$

$$2x = 70 \quad \checkmark$$

$$x = 35 \quad \checkmark$$

$$x + 70 \Rightarrow 35 + 70 = 105$$

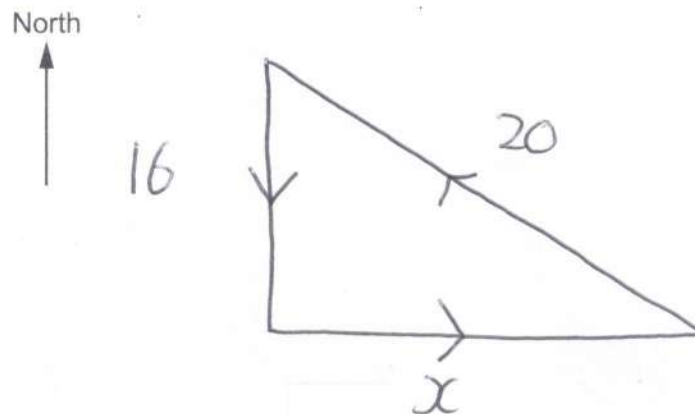
$$180 - 105 \quad \checkmark$$

$$y = 75 \quad \checkmark$$



6. (a) Sam cycled south for 16 km.
He then turned and cycled **east**.
When he stopped for a rest, the shortest distance back to his starting point was 20 km.

Calculate how many kilometres Sam cycled while travelling east. [3]



$$x = \sqrt{20^2 - 16^2} \quad \checkmark$$

$$= \sqrt{400 - 256} \quad \checkmark$$

$$= \sqrt{144} = 12 \quad \checkmark$$

- (b) Sam cycled the 20 km back to his starting point at a constant speed of 25 km/h.

How many minutes did this take? [2]

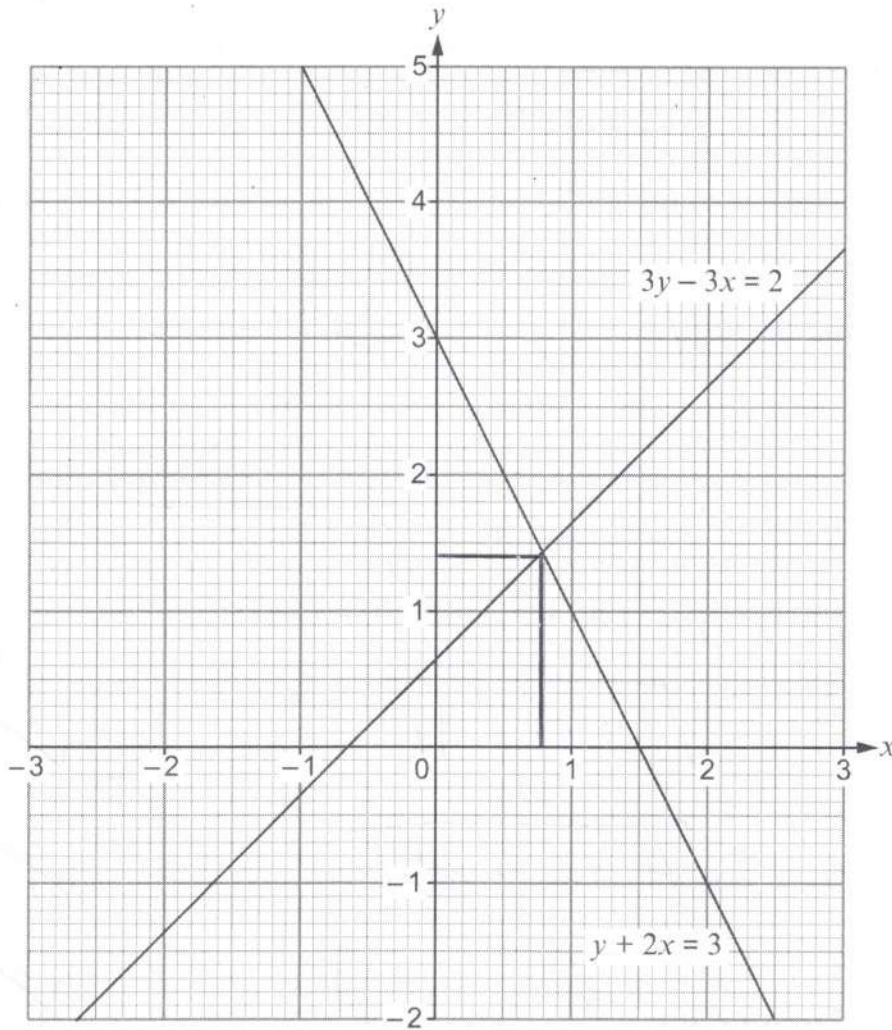
$$25 \text{ km} \rightarrow 60 \text{ min} \quad \checkmark$$

$$5 \text{ km} \rightarrow 12 \text{ mins} \quad \checkmark$$

$$20 \text{ km} \rightarrow 48 \text{ mins} \quad \checkmark$$



7. (a)



Use the diagram to solve the following simultaneous equations.

$$3y - 3x = 2$$

$$y + 2x = 3$$

Give your answers correct to 1 decimal place.

[2]

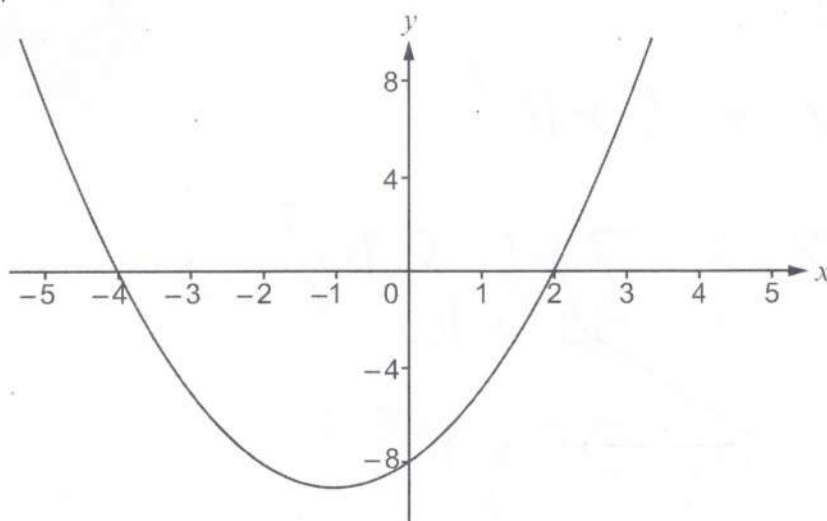
✓
✓

$$x = \frac{0.8}{(\text{or } 0.7)}$$

$$y = \frac{1.4}{(\text{or } 1.5)}$$



- (b) The diagram shows the curve $y = x^2 + 2x - 8$.



- (i) Write down the y -intercept of the curve.

-8

✓

[1]

- (ii) Find the coordinates of the turning point of the curve.

[2]

$$\frac{-4+2}{2} = -1$$

$$y = 1 - 2 - 8$$

(-1, -9)

✓ ✓

- (iii) Use the diagram to solve $x^2 + 2x - 8 = 0$.

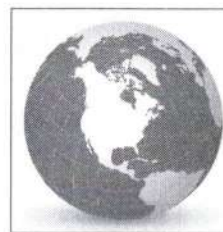
[1]

$$x = -4 \text{ or } x = 2$$

✓



8. The surface area of the Earth is $5.101 \times 10^8 \text{ km}^2$.
The Earth's oceans are 70.9% of this surface area.



Estimate the surface area of the Earth's oceans.
Give your answer in standard form.

[3]

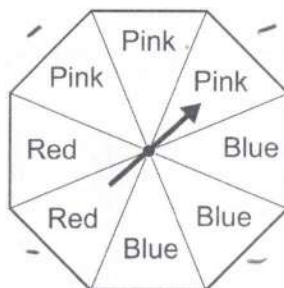
$$10\% = 5 \times 10^7$$

$$70\% = 7 \times 5 \times 10^7$$

$$= 35 \times 10^7$$

$$= 3.5 \times 10^8$$

9.



3P 2R

3B

$$R = \frac{2}{8} = \frac{1}{4}$$

The diagram shows a fair spinner.
Eve spins it twice.

What is the probability that the spinner lands on red both times?

[2]

$$RR = \frac{1}{4} \times \frac{1}{4} = \frac{1}{16}$$



10. (a) In an athletics club:
- 20 of the female athletes have a mean height of 170 cm
 - 30 of the male athletes have a mean height of 180 cm.

What is the mean height of these 50 athletes?

[4]

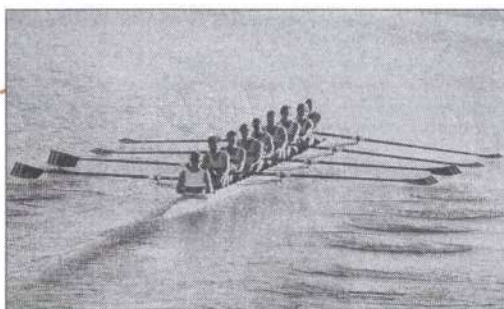
$$170 \times 2 \times 10 = 3400 \quad \checkmark$$

$$180 \times 3 \times 10 = 5400 \quad \checkmark$$

$$\underline{8800} \quad \checkmark$$

$$\checkmark \quad \frac{8800}{50} = \frac{176}{5)880} \quad 176 \text{ cm } \checkmark$$

- (b) A boat crew has 8 rowers and a cox who steers.



The heights, in cm, of the 9 people in the crew are as follows.

150 183 193 201 203 198 201 188 193

The mean of these heights is 190 cm.

Explain why the mean is not the best average to use for this data set.

[1]

The mean is affected by the 150/cox
etc \checkmark



11. The table shows some information about the cost per person to take a boat across a river.

| | |
|--------------|-----|
| Adults (£) | a |
| Children (£) | c |



The Jones family of 4 adults and 1 child pay £9.50 to take the boat.
The Patel family of 5 adults and 2 children pay £13 to take the boat.

The Lee family has 3 adults and 2 children.

How much does the Lee family pay to take the boat?
You must use an algebraic method and show all your working.

[5]

$$\begin{array}{r}
 \checkmark \quad 4a + 1c = 9.5 \quad (\times 2) \\
 \quad 5a + 2c = 13 \\
 \rightarrow \quad 8a + 2c = 19 \quad \checkmark \\
 \hline
 \quad 3a \quad = 6 \quad \checkmark \\
 \hline
 \pounds 8 + 1c = \pounds 9.50 \quad c = \pounds 1.50 \quad \checkmark
 \end{array}$$

$$\begin{array}{r}
 \text{Lee} \rightarrow 3 \times 2 + 2 \times 1.5 \\
 \quad \quad 6 \quad + 3
 \end{array}$$

The Lee family pays

$\pounds 9$

✓



12. (a) Circle the equation of a line parallel to the line $y = 4x + 5$. [1]

$y = -\frac{1}{4}x + 5$ $y = 4x - 5$ $y = -4x + 5$ $y = \frac{1}{4}x - 5$ $4y = x + 5$

- (b) The gradient of the line which passes through the points $(a, 3)$ and $(2a, 9)$ is $\frac{3}{4}$.

Find the value of a . [3]

$$\checkmark \frac{9-3}{2a-a} = \frac{6}{a} = \frac{3}{4} \quad \checkmark$$

$$24 = 3a$$

$$a = 8 \quad \checkmark$$

13. (a) (i) Find the next term of the following Fibonacci-type sequence. [1]

0 2 2 4 6 10 ✓

- (ii) Here are the first 4 terms of a sequence.

$\sqrt{3}$

1

$\frac{1}{\sqrt{3}}$

$\frac{1}{3}$

$\frac{1}{3\sqrt{3}}$ ✓

$\frac{1}{9}$ ✓

Find the 6th term of this sequence.
Simplify your answer. [2]

$$\times \frac{1}{\sqrt{3}}$$

- (b) Find the n th term of the following sequence. [2]

-3 0 5 12 21

3 5 7 9

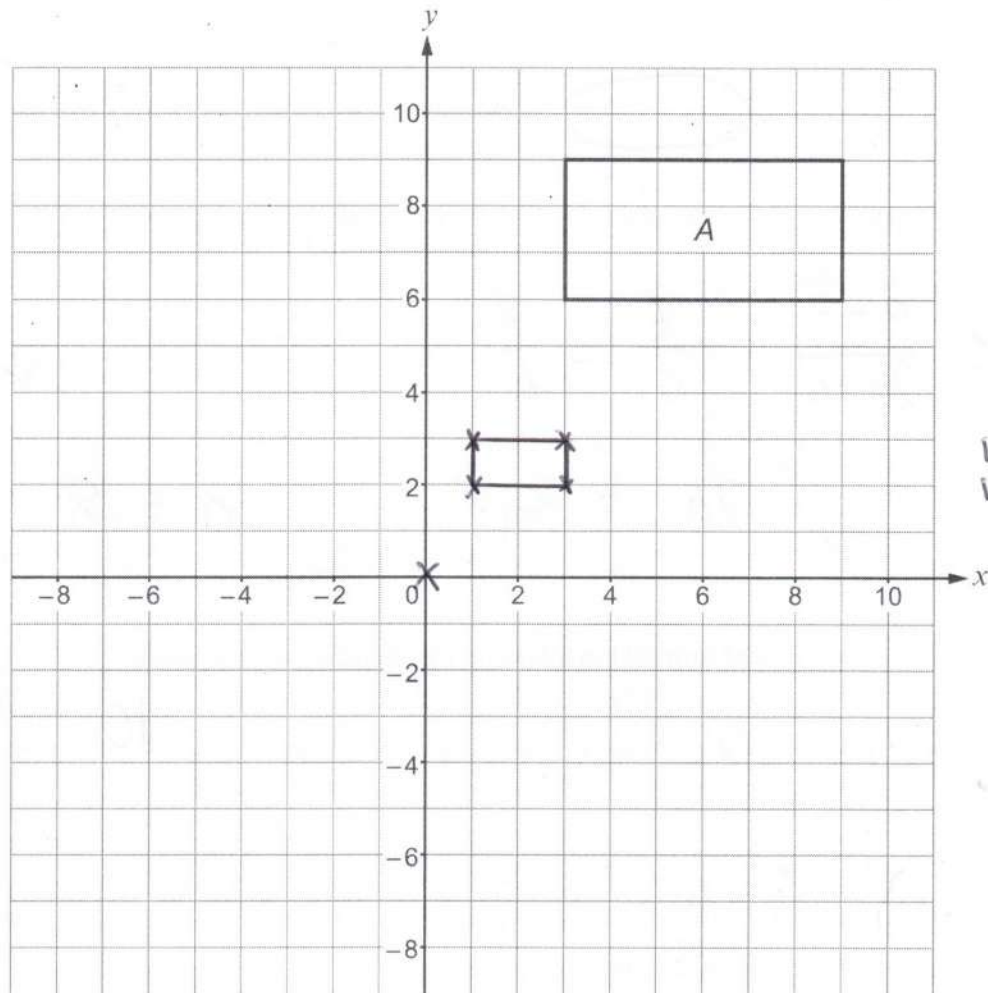
2 2 2

n^2 1 4 9 16

$$n^2 - 4 \quad \checkmark \checkmark$$



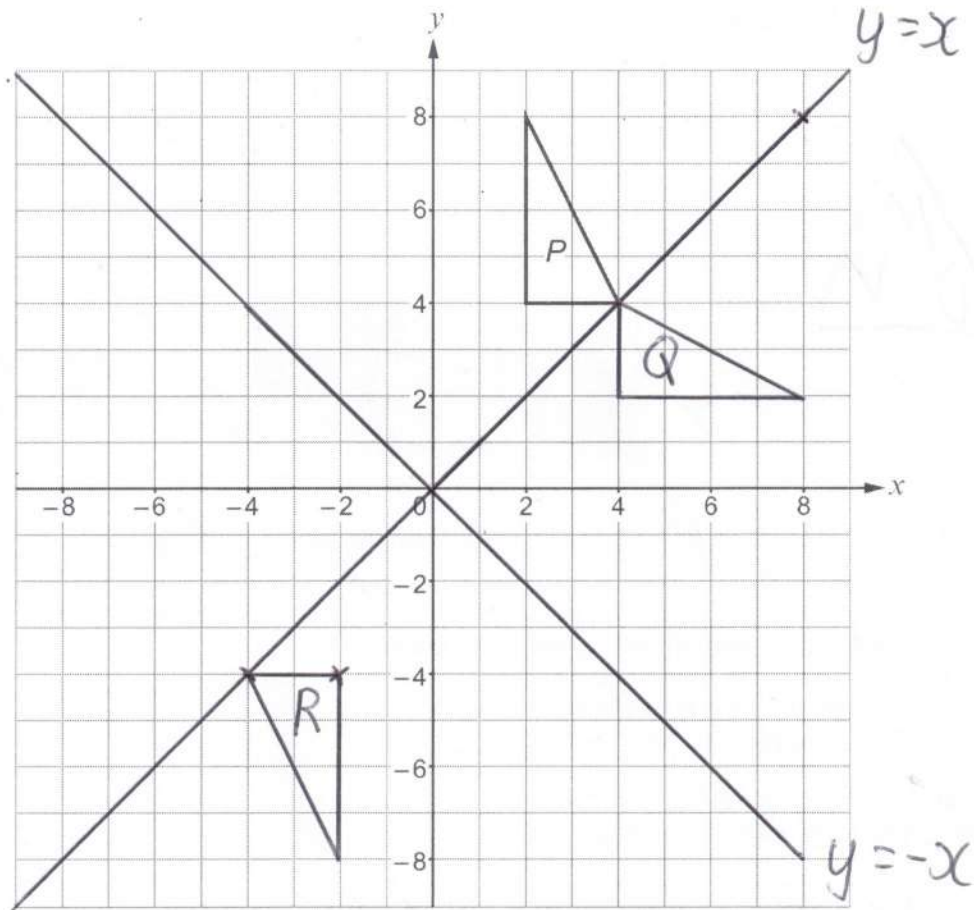
14. (a)



Draw the enlargement of rectangle A with scale factor $\frac{1}{3}$ and centre $(0, 0)$. [2]



(b)



Triangle P is reflected in the line $y = x$.
The image is triangle Q .

Triangle Q is reflected in the line $y = -x$.
The image is triangle R .

Describe a **single** transformation that maps triangle P to triangle R .

[3]

Rotation, 180 , about $(0,0)$ ✓✓✓

or enlargement, $sf = -1$, centre $(0,0)$



15. A small tank is a cuboid. It has a square base of side 20 cm. The tank contains some liquid but is not full.

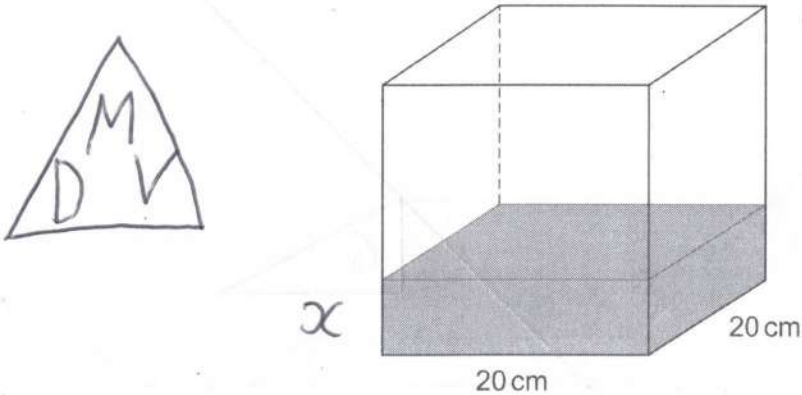


Diagram not drawn to scale

More of the same type of liquid is added to the tank:

- The total mass of the liquid in the tank is now 5400 grams.
- The depth of the liquid has increased by 50%.
- The density of the liquid is 0.9 g/cm^3 .

Calculate the **original** depth of the liquid.
You must show all your working.

[5]

$$\text{Orig. } V = 20 \times 20 \times x = 400x \quad \checkmark \checkmark$$

$$\text{New } V = 20 \times 20 \times 1.5x = 600x$$

$$D = \frac{M}{V}$$

so

$$0.9 = \frac{5400}{600x} \quad \checkmark \checkmark$$

$$0.9x = 9$$

$$x = 10 \quad \checkmark$$



16. (a) Write $13^{-2} \times 13^7$ as a single power of 13.

$$13^5$$

✓

[1]

(b) Calculate the value of $(8^{-1})^{\frac{1}{3}}$.

$$= 8^{-\frac{1}{3}} = \frac{1}{\sqrt[3]{8}} = \frac{1}{2}$$

✓

✓

[2]

(c) $3^{\frac{5}{a}} = b\sqrt{3}$ where a and b are integers.

Find the value of a and the value of b .

[2]

$$a\sqrt{3^5} = b\sqrt{3}$$

$$a\sqrt{3^4 \times 3} = b\sqrt{3}$$

✓

$$\sqrt{3^4} = 3^2 = 9 \quad \text{so} \quad \begin{cases} a=2 \\ b=9 \end{cases}$$

✓

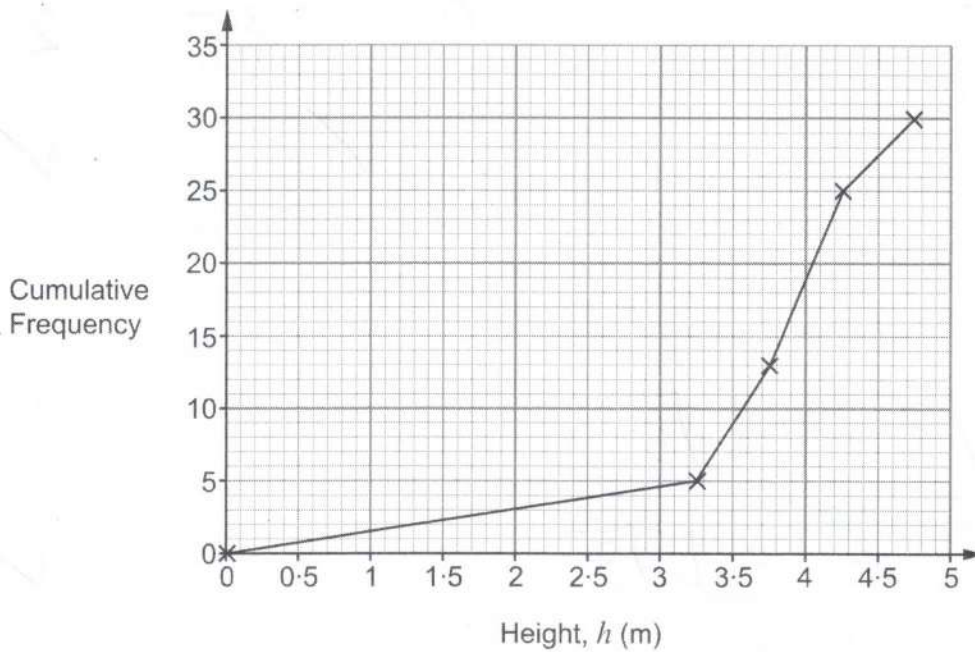
$$3^{\frac{5}{10}} = \boxed{\text{OR}} \quad 3^{\frac{1}{2}} = \sqrt{3} \quad \text{so} \quad \begin{cases} a=10 \\ b=1 \end{cases}$$



17. (a) Gracie has collected data about the heights of 30 giant sunflowers. The table shows her results.

| Height, h (m) | $3 < h \leq 3.5$ | $3.5 < h \leq 4$ | $4 < h \leq 4.5$ | $4.5 < h \leq 5$ |
|-----------------|------------------|------------------|------------------|------------------|
| Frequency | 5 | 8 | 12 | 5 |

Gracie attempts to draw a cumulative frequency diagram.



Make **two** different criticisms of Gracie's diagram. [2]

1. Should not be joined to (0,0) ✓

2. Midpoints have been used etc ✓



- (b) Gracie also collects data about the amount of money each of a group of 40 gardeners spent on their gardens during the months of April and May. The table shows the data for April.

width 30 10 10 10 20

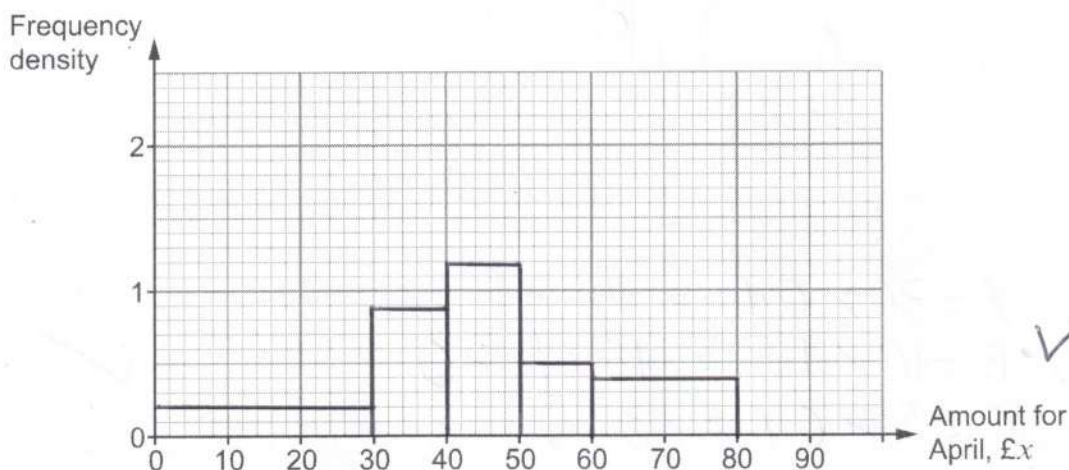
| Amount for April, (£.x) | $0 < x \leq 30$ | $30 < x \leq 40$ | $40 < x \leq 50$ | $50 < x \leq 60$ | $60 < x \leq 80$ |
|-------------------------|-----------------|------------------|------------------|------------------|------------------|
| Frequency | 6 | 9 | 12 | 5 | 8 |

Area
fd =

0.2 0.9 1.2 0.5 0.4

✓✓

- (i) Draw a histogram to represent the data for April. [4]



.....

.....

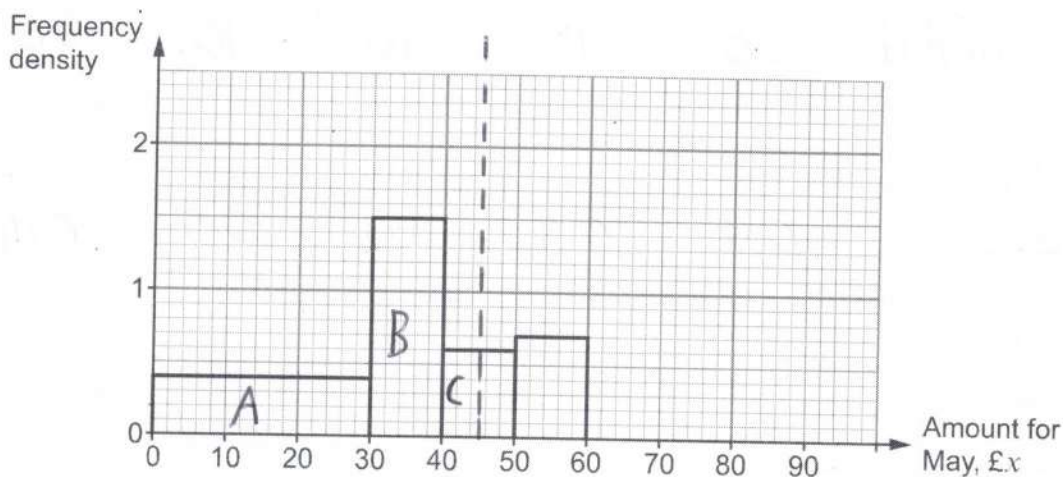
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.....

.....



(ii) The histogram below represents the data for May.



Calculate an estimate of how many more of the 40 gardeners spent £45 or less in May than spent £45 or less in April?
You must show all your working. [3]

$A = 30 \times 0.4 = 12$
 $B = 10 \times 1.5 = 15$
 $C = 5 \times 0.6 = 3$

} 30 ✓

Apr = $6 + 9 + 6 = 21$

$30 - 21 = 9$ ✓



18. (a)

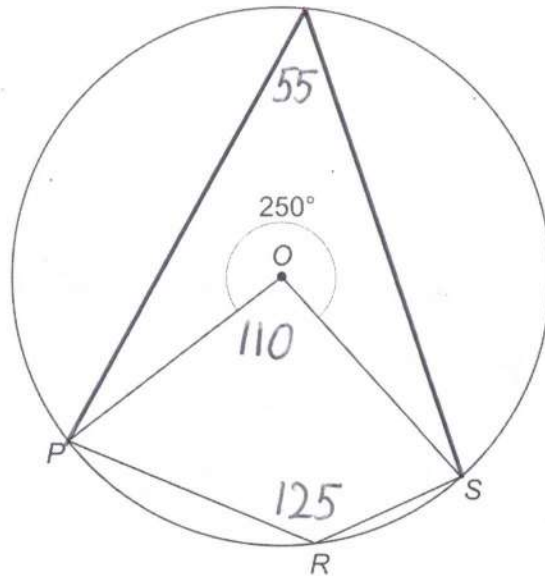


Diagram not drawn to scale

The diagram shows a circle, centre O .
Points P , R and S are on the circumference of the circle.

Reflex angle $\widehat{POS} = 250^\circ$.

$\widehat{OPR} : \widehat{OSR} = 2 : 3$.

Calculate the size of \widehat{OPR} .
You must show all your working.

[3]

$$360 - 110 - 125 = 125$$

$$\widehat{OPR} = \frac{2}{5} \times 125$$

$$= 2 \times 25$$

$$= 50^\circ$$



(b)

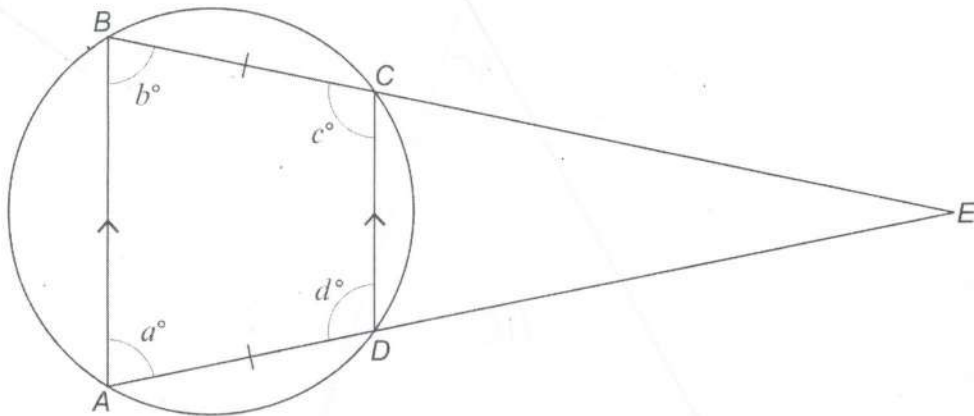


Diagram not drawn to scale

 ABE is an isosceles triangle. AB is parallel to DC so that $ABCD$ is an isosceles trapezium.Prove that $ABCD$ is always a cyclic quadrilateral.

State any reasons that you use in your proof.

[3]

$$a = b \text{ and } c = d \text{ (isosceles)} \quad \checkmark$$

$$\begin{aligned} a + d &= 180 \\ b + c &= 180 \end{aligned} \quad \text{(co-interior)} \quad \checkmark$$

hence

$$a + c = 180$$

$$b + d = 180$$

opposite angles in a cyclic
quadrilateral sum to 180 \checkmark



19. You are given that y is inversely proportional to x^2 .
When $x = 4$, $y = 3$.

(a) Find a formula for y in terms of x .

[3]

$$y = \frac{k}{x^2} \quad \checkmark$$

$$3 = \frac{k}{16}$$

$$k = 48 \quad \checkmark$$

$$y = \frac{48}{x^2} \quad \checkmark$$

(b) (i) Use your formula to find the value of y when $x = 8$.

[1]

$$y = \frac{48}{64} \quad \checkmark \text{OE}$$

(ii) Use your formula to find the positive value of x when $y = 1200$.

[2]

$$1200 = \frac{k}{x^2}$$

$$x^2 = \frac{48}{1200} = \frac{4}{100} = \frac{1}{25} \quad \checkmark$$

$$x = \frac{1}{5} \quad \checkmark$$



20. Write $3.\dot{2}\dot{1}$ as a fraction.
Give your answer as a mixed number in its simplest form. [3]

$$\begin{aligned} x &= 3.\dot{2}\dot{1} \\ 100x &= 321.\dot{2}\dot{1} \\ \hline 99x &= 21 \\ \hline x &= \frac{21}{99} = \frac{7}{33} \end{aligned}$$

$3\frac{7}{33}$

21. In this question all lengths are in centimetres.

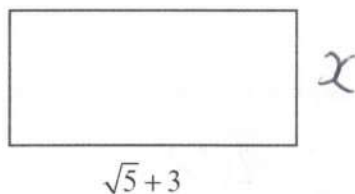


Diagram not drawn to scale

The length of this rectangle is $\sqrt{5}+3$.

The perimeter of the rectangle is $8\sqrt{5}-2$.

Calculate the exact area of this rectangle. [5]

$$2x = 8\sqrt{5}-2 \quad - (2\sqrt{5}+6) \quad \checkmark$$

$$2x = 6\sqrt{5}-8$$

$$x = 3\sqrt{5}-4 \quad \checkmark$$

$$A = (\sqrt{5}+3)(3\sqrt{5}-4) \quad \checkmark$$

$$= 3\sqrt{25} - 4\sqrt{5} + 9\sqrt{5} - 12$$

$$= 15 - 12 + 5\sqrt{5} = 3 + 5\sqrt{5} \quad \checkmark$$



22.

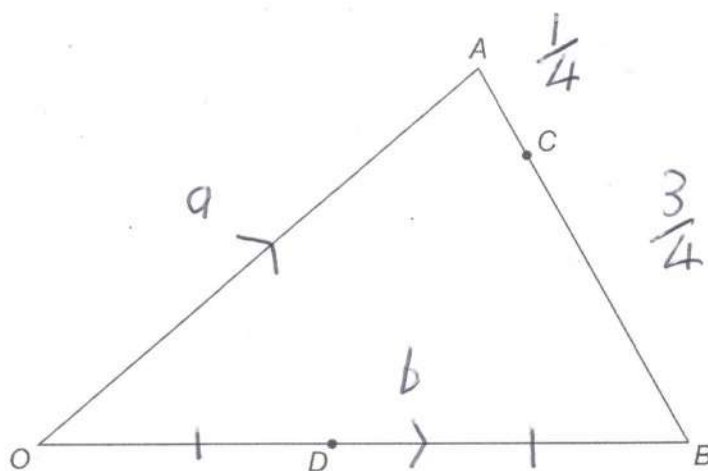


Diagram not drawn to scale

 $\mathbf{OA = a}$ and $\mathbf{OB = b}$.C is the point on AB such that $\mathbf{AC : AB = 1 : 4}$.

D is the mid-point of OB.

Find \mathbf{DC} in terms of \mathbf{a} and \mathbf{b} .

Give your answer in its simplest form.

[4]

$$\vec{BA} = -b + a \quad \checkmark$$

$$\vec{DC} = \vec{DB} + \vec{BC}$$

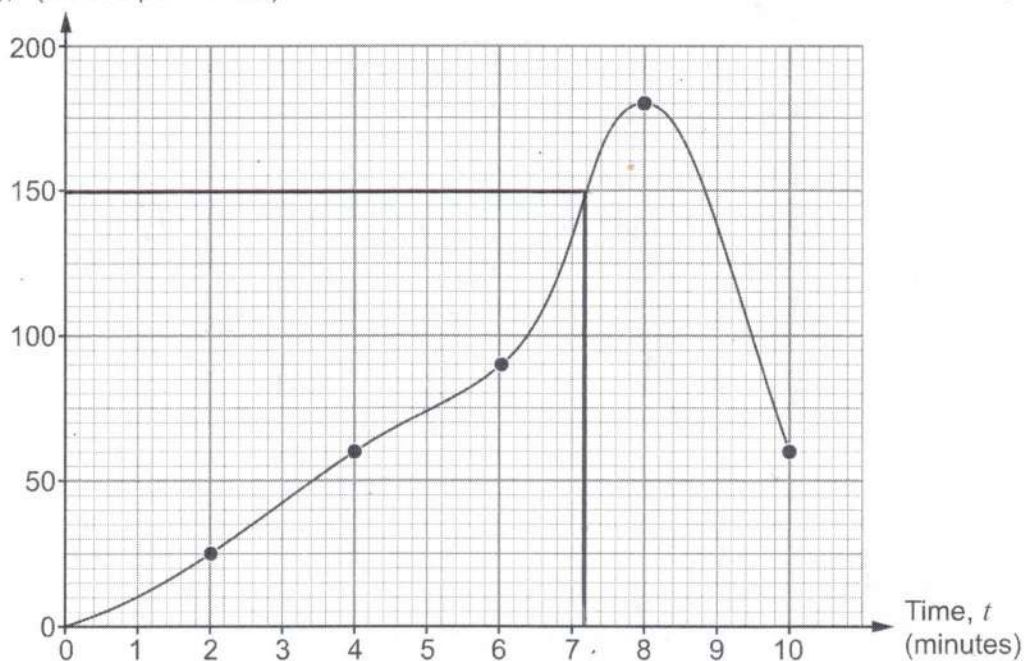
$$= \frac{1}{2}b + \frac{3}{4}(-b + a) \quad \checkmark \checkmark$$

$$= \frac{1}{2}b - \frac{3}{4}b + \frac{3}{4}a$$

$$= \frac{3}{4}a - \frac{1}{4}b \quad \checkmark$$



23.

Velocity, v (metres per minute)

The diagram shows a velocity-time graph for the first 10 minutes of a cyclist's journey. The velocity is given in metres per minute and the time is given in minutes.

How many minutes after the start of the journey did the cyclist first travel at a velocity of 9 kilometres per hour? [4]

$$\begin{aligned}
 9 \text{ km} &\rightarrow 1 \text{ hr} \\
 9000 \text{ m} &\rightarrow 60 \text{ mins} \\
 150 \text{ m} &\text{ per } 1 \text{ min}
 \end{aligned}$$

$$7.2 \text{ mins}$$



24. (a) Solve the equation $5x^2 - 8x - 1 = 0$.

Give your answers in the form $\frac{m \pm \sqrt{n}}{5}$, where m and n are integers. [3]

$$x = \frac{8 \pm \sqrt{64 - 4 \times 5 \times -1}}{10} \quad \checkmark$$

$$= \frac{8 \pm \sqrt{84}}{10} \quad \checkmark$$

$$= \frac{8 \pm \sqrt{4 \times 21}}{10} = \frac{4 \pm \sqrt{21}}{5} \quad \checkmark$$

(b) Use factorisation to solve the following equation. [6]

$$\frac{4}{x-1} = 3 + \frac{2}{x}$$

$$4x = 3x(x-1) + 2(x-1) \quad \checkmark \checkmark$$

$$0 = 3x^2 - 3x + 2x - 2 - 4x \quad \checkmark$$

$$0 = 3x^2 - 5x - 2 \quad \checkmark$$

$$0 = (3x+1)(x-2) \quad \checkmark$$

$$x = -\frac{1}{3}, \quad x = 2 \quad \checkmark$$

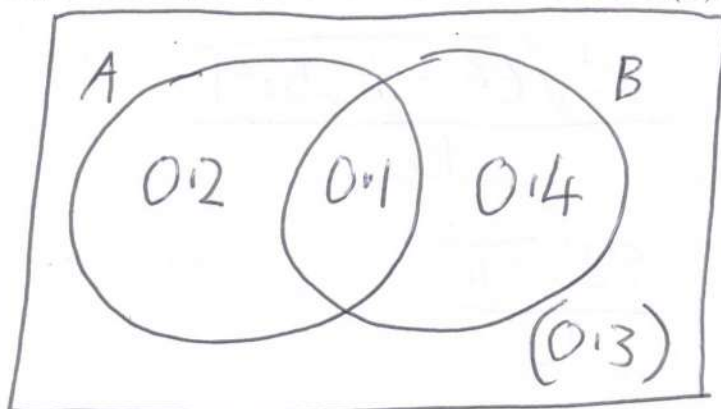


25. The following probabilities are given for events A and B.

$$P(A) = 0.3, \quad P(A \cup B) = 0.7, \quad P(A \cap B) = 0.1$$

(a) By drawing a Venn diagram, or otherwise, find the value of $P(B)$.

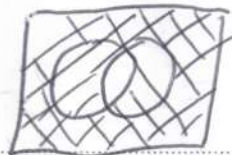
[3]



$$P(B) = 0.5$$

(b) Find $P(A' \cup B')$.

$$A' \cup B' =$$



or $1 - P(A \cap B)$

$$= 0.9$$

END OF PAPER

