

Apart from questions 6, 8, 13b and 24 (where the mark scheme states otherwise) the correct answer, unless clearly obtained from an incorrect method, should be taken to imply a correct method.

Question	Working	Answer	Mark	Notes
1	$\frac{5}{3} + \frac{11}{4}$ $\frac{20}{12} + \frac{33}{12}$ $\frac{53}{12} = 4\frac{5}{12}$ <p>Alternative method</p> $\frac{2}{3} + \frac{3}{4} = \frac{8}{12} + \frac{9}{12}$ $\frac{17}{12} = 1\frac{5}{12}$ $1\frac{5}{12} + 1 + 2 = 4\frac{5}{12}$	Shown	3	<p>M1 converts to improper fractions</p> <p>M1 converts to fractions with the same common denominator</p> <p>A1 Dep on M2</p> <p>M1 correct method to add proper fractions</p> <p>M1</p> <p>A1 Dep on M2</p>

Question	Working	Answer	Mark	Notes
2	$\frac{3}{4} \times 60 (= 45) \text{ or } \frac{1}{4} \times 60 (= 15) \text{ OR } \frac{3}{4} \times \frac{3}{5} \left(= \frac{9}{20} \right)$ $\frac{3}{5} \times "45" (= 27) \text{ or } \frac{4}{5} \times "15" (= 12) \text{ OR}$ $\frac{1}{4} \times \frac{4}{5} \left(= \frac{4}{20} \right)$ $\frac{"27" + "12"}{60} \text{ OR } "\frac{9}{20}" + "\frac{4}{20}"$	$\frac{13}{20}$	4	M1 M1 M1 For a complete method A1 oe
3	$14^2 - 10^2 (= 96)$ $"96" + 5^2 (= 121)$ $\sqrt{"121"}$	11	4	M1 M1 M1 A1
4	$(a =) 40 - 14 (= 26)$ e.g. $\frac{"26" + b}{2} = 30 \text{ or } 30 + (30 - "26")$	26 34	3	M1 Method to find a M1 Method to find b A1

Question	Working	Answer	Mark	Notes	
5	$30.5 \div 8 (= 3.8125)$ OR $60 \div 8 (= 7.5)$ $"3.8125" \times 60$ OR $30.5 \times "7.5"$	228.75	3	M1 M1 A1	M2 for $30.5 \div \frac{8}{60}$ oe accept 229, 228.8
6	$3x + 10 = x + 52$ $3x - x = 52 - 10$ or $2x = 42$ or $x = 21$ $y = 180 - 2 \times ("21" + 52)$ or $y = 180 - 2 \times (3 \times "21" + 10)$ or $y = 180 - ("21" + 52) - (3 \times "21" + 10)$	34	4	M1 M1 M1 A1	for equating the expressions for angle P and angle Q for isolating the terms in x for a complete method dep on M2
7	eg $\frac{187}{147}$ or $\frac{147}{187}$ or $\frac{90}{187}$ or $\frac{187}{90}$ eg $90 \div \frac{187}{147}$ or $90 \times \frac{147}{187}$ or $147 \times \frac{90}{187}$ or $147 \div \frac{187}{90}$	71	3	M1 M1 A1	for an appropriate scale factor, candidates may work in either cm or m for a complete method, candidates may work in either cm or m 70.7 – 71

Question	Working	Answer	Mark	Notes
8	eg $8x + 4y = 18 +$ or $4x + 2y = 9 -$ $x - 4y = 9$ $4x - 16y = 36$ or $4(9 + 4y) + 2y = 9$ eg $4 \times "3" + 2y = 9$ or $4x + 2 \times "-1.5" = 9$ or $x = 9 + 4 \times "-1.5"$	$x = 3,$ $y = -1.5$	3	M1 correct method to eliminate x or y : coefficients of x or y the same and correct operation to eliminate the selected variable (condone any one arithmetic error in multiplication) or writing x or y in terms of the other variable and correctly substituting M1 (dep) correct method to find second variable using their value from a correct method to find first variable or for repeating above method to find second variable A1 oe, dep first M1
9 (a)		4.8×10^{11}	1	B1
(b)		$2^{14} \times 3 \times 5^{10}$	3	B3 for the correct answer B2 for an answer in the form $2^m \times 3 \times 5^n$, where m and n are positive integers B1 for at least 2 correct steps in repeated prime factorisation (including tree diagram)
(c)		29 296 875	1	B1 Accept 3×5^{10} , 2.9296875×10^7

Question	Working	Answer	Mark	Notes
10	$\pi \times \left(\frac{12}{2}\right)^2 (=113....)$ or $\pi \times \left(\frac{12}{2} - 2\right)^2 (=$ $50.2....)$ or $\pi \times \left(\frac{12}{2}\right)^2 \div 2 (=56.5...)$ or $\pi \times \left(\frac{12}{2} - 2\right)^2 \div 2 (=25.1...)$ eg $(\pi \times 6^2 - \pi \times 4^2) \div 2$ oe	10π	3	M1 M1 for a complete method A1

Question	Working	Answer	Mark	Notes
11	$12 \times 5.5 (= 66)$ $\frac{"66"+18}{20}$	4.2	3	M1 M1 for a complete method A1
12 (a)		$\frac{n}{2n-1}$	2	M1 for $2n \pm k$ oe as the denominator A1 oe
(b)	$(2n-1)^2 = 4n^2 - 4n + 1$ $4(n^2 - n) + 1 \text{ or } \frac{4n^2 - 4n + 1}{4} = n^2 - n + \frac{1}{4}$	Proved	3	M1 or $(2n+1)^2 = 4n^2 + 4n + 1$ ft on $2n \pm k$ (k non zero) M1 or $4(n^2 + n) + 1 \text{ or } \frac{4n^2 + 4n + 1}{4} = n^2 + n + \frac{1}{4}$ A1 Conclusion

Question	Working	Answer	Mark	Notes
13 (a)		$3x^2 - 2x - 8$	2	B2 (B1 for at least 1 correct non zero term)
(b)	$"3x^2 - 2x - 8" = 0$ $(3x + 4)(x - 2) (=0)$ or $x = \frac{2 \pm \sqrt{100}}{2 \times 3}$ or $x = \frac{2 \pm \sqrt{(-2)^2 - 4 \times 3 \times (-8)}}{2 \times 3}$	$-\frac{4}{3}, 2$	3	M1 Dep on at least B1, ft on M marks only dep on $\frac{dy}{dx}$ being a 3 term quadratic M1
(c)	At $x = 2, y = 2^3 - 2^2 - 8 \times 2 + 12 (= 0)$ or at $x = -\frac{4}{3},$ $y = \left(-\frac{4}{3}\right)^3 - \left(-\frac{4}{3}\right)^2 - 8 \times \left(-\frac{4}{3}\right) + 12$ $\left(= \frac{500}{27}\right)$	Shown	2	A1 (dep 2nd M1) M1 Substitutes at least one of $-\frac{4}{3}$ or 2 or their answer from (b) into $(y =)x^3 - x^2 - 8x + 12$ A1 must show that (2,0) is a turning point on the curve and give concluding statement

Question	Working	Answer	Mark	Notes	
14 (a)		97	1	B1	96 - 98
(b)		Correct graph	2	M1	for at least 4 points plotted correctly at end of interval or for all 6 points plotted consistently within each interval at the correct height
				A1	accept curve or line segments accept curve that is not joined to (0, 0)
(c)		14	2	M1	A line drawn at CF = 60 to meet at least one curve or sight of “55” or “69”
				A1	13 - 15 ft candidate's CFD

Question	Working	Answer	Mark	Notes	
15 (a)		$81x^8y^{20}$	2	B2	(B1 two terms correct in a product of 3 terms)
(b)	$4n(n^2 + 2n - 15)$ or $(4n^2 - 12n)(n + 5)$ or $(4n^2 + 20n)(n - 3)$	$4n^3 + 8n^2 - 60n$	2	M1	For a correct partial expansion (may be unsimplified e.g $4n(n^2 + 5n - 3n - 15)$)
				A1	
(c)		$(2c - 3d)(2c + 3d)$	1	B1	
(d)	$\frac{(4 - x)(3 - x)}{x(4 - x)}$ or $\frac{(x - 4)(x - 3)}{x(4 - x)}$	$\frac{3 - x}{x}$	3	M1	for either numerator or denominator factorised correctly
				M1	for both numerator and denominator factorised correctly
				A1	oe

Question	Working	Answer	Mark	Notes
16 (a)	$\frac{2}{12} \times \frac{1}{11}$	$\frac{1}{66}$	2	M1
(b)	Any two of $\frac{7}{12} \times \frac{3}{11} \left(= \frac{21}{132} \right)$ or $\frac{7}{12} \times \frac{2}{11} \left(= \frac{14}{132} \right)$ or $\frac{3}{12} \times \frac{2}{11} \left(= \frac{6}{132} \right)$ $2 \times \frac{7}{12} \times \frac{3}{11} + 2 \times \frac{7}{12} \times \frac{2}{11} + 2 \times \frac{3}{12} \times \frac{2}{11}$ Alternative method $\frac{7}{12} \times \frac{6}{11} \left(= \frac{42}{132} \right)$ and $\frac{3}{12} \times \frac{2}{11} \left(= \frac{6}{132} \right)$ $1 - \frac{2}{12} \times \frac{1}{11} - \frac{7}{12} \times \frac{6}{11} - \frac{3}{12} \times \frac{2}{11}$	$\frac{41}{66}$	3	A1 M1 for any two correct M1 for a complete method A1 oe M1 both correct M1 for a complete method A1 SC B2 for an answer of $\frac{41}{72}$ oe

Question	Working	Answer	Mark	Notes
17 (a)	$2\pi r^2 + 2\pi r \times 2r$	$6r^2$	2	M1
(b)	S.A. $6\pi r^2 : 4\pi r^2 = 3 : 2$	Shown	3	A1 M1 ft their answer from (a), must be in terms of r . Ratios could be seen as fractions throughout eg $\frac{3}{2}$
	$V_c : V_s = 2\pi r^3 : \frac{4}{3} \pi r^3$			M1
	$= 3 \times 2 : 4 = 3 : 2$			A1 oe eg ratios could be $\frac{3}{2} : 1$

Question	Working		Answer	Mark	Notes
18	$\frac{\sqrt{8}}{\sqrt{8}-2} \times \frac{\sqrt{8}+2}{\sqrt{8}+2}$ $\frac{\sqrt{8}(\sqrt{8}+2)}{8-4} = \frac{8+2\sqrt{8}}{4} = \frac{8+4\sqrt{2}}{4}$ $= 2 + \sqrt{2}$		Shown	3	M1 or $\frac{2\sqrt{2}}{2\sqrt{2}-2}$ or $\frac{\sqrt{2}}{\sqrt{2}-1}$ M1 or $\frac{\sqrt{2}}{\sqrt{2}-1} \times \frac{\sqrt{2}+1}{\sqrt{2}+1}$ A1 (dep on M2) Conclusion - need not state the value of n
19	Angle $BCE = 73^\circ$ Angle $DEB = 73^\circ$ and Angle $DCB = 180-73 (=107^\circ)$ Angle $DCE = 34^\circ$ eg <u>Alternate segment</u> theorem Opposite angles of a <u>cyclic quadrilateral</u> sum to 180° <u>Alternate angles</u> are equal Angles in the <u>Same segment</u> are equal <u>Angles</u> in a <u>triangle</u> sum to 180	Angle $BDE = 73^\circ$ Angle $DEB = 73^\circ$ and Angle $DBE = 180-73 \times 2 (=34^\circ)$	34	5	M1 angles may be written on the diagram M1 A1 B2 for a full set of reasons relevant to their method (B1 for at least one relevant circle theorem)

Question	Working	Answer	Mark	Notes
20	<p>Let N be the midpoint of BC</p> <p>Let sides of cube have length $2a$ cm</p> <p>$AN^2 = 4a^2 + a^2 (= 5a^2)$ or $AM^2 = 4a^2 + a^2 + 4a^2 (= 9a^2)$</p> <p>eg $\tan MAN = \frac{2a}{\sqrt{5a^2}}$ or $\sin MAN = \frac{2a}{\sqrt{9a^2}}$</p>	41.8	4	<p>B1 for recognising that required angle is MAN (could be marked on a diagram)</p> <p>M1 any $a > 0$ (a could be a number or a letter)</p> <p>M1 correct trig statement for angle MAN, any $a > 0$ (a could be a number or a letter)</p> <p>A1 41.8 - 41.82</p>
21	<p>$x^2 = 5^2 + y^2 - 2 \times 5 \times y \cos 60^\circ$</p> <p>$(y-1)^2 = 5^2 + y^2 - 5y$ or $x^2 = 5^2 + (x+1)^2 - 5x - 5$</p> <p>$y^2 - 2y + 1 = 25 + y^2 - 5y$ or</p> <p>$x^2 = 5^2 + x^2 + 2x + 1 - 5x - 5$</p> <p>$5y - 2y = 25 - 1$ or $y = 8$ or $3x = 21$ or $x = 7$</p>	20	5	<p>M1 recognising need for the cosine rule</p> <p>M1</p> <p>M1 for expansion of $(y-1)^2$ or $(x+1)^2$ in a correct equation</p> <p>M1 for correct linear equation with correct isolation of terms</p> <p>A1</p>

Question	Working	Answer	Mark	Notes
22	<p>eg $\overrightarrow{EX} = \overrightarrow{ED} + \overrightarrow{DC} + \overrightarrow{CX}$ or $\overrightarrow{EX} = \overrightarrow{EF} + \overrightarrow{FA} + \overrightarrow{AX}$</p> <p>$\overrightarrow{DC} = -\mathbf{b} + \mathbf{a}$ or $\overrightarrow{CX} = -\mathbf{b} + \mathbf{a}$ or $\overrightarrow{FA} = -\mathbf{b} + \mathbf{a}$</p> <p>$\overrightarrow{EX} = \mathbf{a} + 2(-\mathbf{b} + \mathbf{a})$</p>	3a – 2b	4	<p>M1 a correct statement for \overrightarrow{EX}</p> <p>M1</p> <p>M1 for a complete method which gives a correct but unsimplified expression for \overrightarrow{EX}</p> <p>A1</p>

Question	Working	Answer	Mark	Notes	
23	(a)		3	M1	for squaring and rearranging correctly to the form $x^2(y^2 - 1) = k^2$
				M1	(dep) for “ $f^{-1}(p)$ ” = k
				A1	
				M1	
				M1	
	(b)		3	A1	
				M1	
				M1	(dep) for rearranging $gf = k$ and isolating correctly the terms in a^2
				A1	oe eg $\sqrt{\frac{k^2}{k-1}}$